



Bharatiya Vidya Bhavan's

Sardar Patel College of Engineering

(A Government Aided Autonomous Institute)

Munshi Nagar, Andheri (West), Mumbai - 400058.

Examinations, April 2022



first year M.Tech - Civil Engg (Constn. mgst.)
Date-13/4/2022

Total points: 100

Duration: 3 Hours

Class: M.TECH(CM).

Semester: I

Program: Civil

Name of the Course: Applied Statistics and Quantitative Techniques Course Code : PC-MTCM-102

Instructions:

1. Q1 and Q2 are compulsory
2. Draw neat diagrams
3. Assume suitable data if necessary and state the clearly.

| Que. No | | Points | CO | BL | PI | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---------|--|--------|-------|-------|-------|------------|-------|--|--|--------|-------|-------|-------|-------|-------|------------|-------|------|----|----|----|----|----|----|-----|--------|----|----|----|----|----|---|-----|-------|----|----|----|----|----|----|-----|----|---|---|-------|
| Q1 (A) | <p>The average number of collisions occurring in a week during the summer months at a particular intersection is 2.00. Assume that the requirements of the Poisson distribution are satisfied.</p> <p>a) What is the probability of no collisions in any week?</p> <p>b) What is the probability that there will be exactly one collision in a week?</p> <p>c) What is the probability of exactly two collisions in a week?</p> <p>d) What is the probability of finding not more than two collisions in a week?</p> <p>e) What is the probability of finding more than two collisions in a week?</p> <p>f) What is the probability of exactly two collisions in a particular two-week interval?</p> | 10 | 1 | 4 | 1.1.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q1(B) | <p>Use Simplex method to solve,</p> <p>Max $Z = 4X_1 + 5X_2 + 9X_3 + 11X_4$</p> <p>Subject to, $X_1 + X_2 + X_3 + X_4 \leq 15$</p> <p>$7X_1 + 5X_2 + 3X_3 + 2X_4 \leq 120$</p> <p>$3X_1 + 5X_2 + 10X_3 + 15X_4 \leq 100$</p> <p>All X_1 to X_4 are equal to or greater than zero.</p> | 10 | 3 | 3 | 3.3.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A2(A) | <p>The following contingency table shows a random sample of 321 fatally injured passenger vehicle drivers by age and gender. The expected frequencies are displayed in parentheses. At $\alpha = 0.05$, can you conclude that the drivers' ages are related to gender in such accidents?</p> <table border="1"><thead><tr><th></th><th colspan="6">Age</th><th></th></tr><tr><th>Gender</th><th>16-20</th><th>21-30</th><th>31-40</th><th>41-50</th><th>51-60</th><th>60 & above</th><th>Total</th></tr></thead><tbody><tr><td>Male</td><td>32</td><td>51</td><td>52</td><td>43</td><td>28</td><td>10</td><td>216</td></tr><tr><td>Female</td><td>13</td><td>55</td><td>33</td><td>21</td><td>10</td><td>6</td><td>105</td></tr><tr><td>Total</td><td>45</td><td>73</td><td>85</td><td>64</td><td>38</td><td>16</td><td>321</td></tr></tbody></table> | | Age | | | | | | | Gender | 16-20 | 21-30 | 31-40 | 41-50 | 51-60 | 60 & above | Total | Male | 32 | 51 | 52 | 43 | 28 | 10 | 216 | Female | 13 | 55 | 33 | 21 | 10 | 6 | 105 | Total | 45 | 73 | 85 | 64 | 38 | 16 | 321 | 10 | 2 | 4 | 1.1.2 |
| | Age | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Gender | 16-20 | 21-30 | 31-40 | 41-50 | 51-60 | 60 & above | Total | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Male | 32 | 51 | 52 | 43 | 28 | 10 | 216 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Female | 13 | 55 | 33 | 21 | 10 | 6 | 105 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Total | 45 | 73 | 85 | 64 | 38 | 16 | 321 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

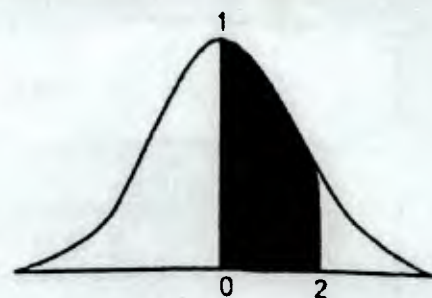
| Q2(B) | <p>John Thompson is the President of Stewarts & Lloyds of India Ltd. John Thompson's problem is to identify whether to expand hi product line by manufacturing and marketing a new product: washing machine.</p> <p>To make a proposal for submitting to his board of directors, Thompson thought of following three alternatives that are available to him.</p> <ol style="list-style-type: none"> 1. To construct a large new plant to manufacture the washing machine 2. To construct a small plant to manufacture the washing machine 3. No plant at all (that is he has the option of not developing the new product line). <p>Thompson determines that there are three possible state of natures:</p> <ol style="list-style-type: none"> 1. The market for the washing machine could be most favorable, meaning that there is a high demand for the product 2. The market for the washing machine could be satisfactorily favorable, meaning that there is a good demand for the product 3. It could be unfavorable, meaning that there is a low demand for the washing machine. <p>John Thompson evaluated the profits associated with various outcomes. The payoff matrix is given below.</p> <p>Using following criteria's, suggest which alternative John Thompson should select</p> <ol style="list-style-type: none"> 1. Maximax (optimistic) 2. Maximin (pessimistic) 3. Criterion of realism (Hurwicz) 4. Equally likely (Laplace) 5. Minimax regret <table border="1"> <thead> <tr> <th rowspan="2">Alternatives</th> <th colspan="3">State of Nature</th> </tr> <tr> <th>most favorable market</th> <th>satisfactorily favorable market</th> <th>Unfavorable market</th> </tr> </thead> <tbody> <tr> <td>Construct a Large plant</td> <td>700000</td> <td>300000</td> <td>150000</td> </tr> <tr> <td>construct a small plant</td> <td>500000</td> <td>450000</td> <td>0</td> </tr> <tr> <td>Do Nothing</td> <td>300000</td> <td>300000</td> <td>300000</td> </tr> </tbody> </table> | Alternatives | State of Nature | | | most favorable market | satisfactorily favorable market | Unfavorable market | Construct a Large plant | 700000 | 300000 | 150000 | construct a small plant | 500000 | 450000 | 0 | Do Nothing | 300000 | 300000 | 300000 | 10 | 2 | 5 | 1.2.2 | | | | | | | | | | | |
|-------------------------|--|---------------------------------|--------------------|----|----|-----------------------|---------------------------------|--------------------|-------------------------|--------|--------|-----------|-------------------------|--------|--------|----|------------|--------|--------|--------|----|----|----|-------|-------|----|----|----|----|----|----|---|---|---|-------|
| Alternatives | State of Nature | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | most favorable market | satisfactorily favorable market | Unfavorable market | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Construct a Large plant | 700000 | 300000 | 150000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| construct a small plant | 500000 | 450000 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Do Nothing | 300000 | 300000 | 300000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q3(A) | <p>Weekly demand of a product is assumed to be normally distributed. Use goodness of fit and following data to test this assumption. Use $\alpha=0.10$, sample mean=24.5 sample std dev=3</p> <table border="1"> <tbody> <tr> <td>18</td><td>20</td><td>22</td><td>27</td><td>22</td><td>26</td><td>25</td><td>25</td><td>27</td><td>25</td></tr> <tr> <td>25</td><td>22</td><td>27</td><td>25</td><td>24</td><td>25</td><td>28</td><td>24</td><td>25</td><td>26</td></tr> <tr> <td>26</td><td>23</td><td>20</td><td>24</td><td>26</td><td>31</td><td>29</td><td>28</td><td>19</td><td>21</td></tr> </tbody> </table> | 18 | 20 | 22 | 27 | 22 | 26 | 25 | 25 | 27 | 25 | 25 | 22 | 27 | 25 | 24 | 25 | 28 | 24 | 25 | 26 | 26 | 23 | 20 | 24 | 26 | 31 | 29 | 28 | 19 | 21 | 8 | 2 | 4 | 1.2.3 |
| 18 | 20 | 22 | 27 | 22 | 26 | 25 | 25 | 27 | 25 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 25 | 22 | 27 | 25 | 24 | 25 | 28 | 24 | 25 | 26 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 26 | 23 | 20 | 24 | 26 | 31 | 29 | 28 | 19 | 21 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q3(B) | <p>Eight coins were tossed 256 times and following results were obtained. Are coins biased? Use chi-square test.</p> <table border="1"> <thead> <tr> <th>No. of heads</th> <th>0</th> <th>1</th> <th>2</th> <th>3</th> <th>4</th> <th>5</th> <th>6</th> <th>7</th> <th>8</th> </tr> </thead> <tbody> <tr> <td>frequency</td> <td>2</td> <td>6</td> <td>30</td> <td>52</td> <td>67</td> <td>56</td> <td>32</td> <td>10</td> <td>1</td> </tr> </tbody> </table> <p>Following table gives monthly sales of certain firm in three states by its four</p> | No. of heads | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | frequency | 2 | 6 | 30 | 52 | 67 | 56 | 32 | 10 | 1 | 6 | 2 | 5 | 1.2.2 | | | | | | | | | | |
| No. of heads | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| frequency | 2 | 6 | 30 | 52 | 67 | 56 | 32 | 10 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | |

| Q3(C) | salesmen. Set up ANOVA | <table border="1"><tr><th>States</th><th colspan="4">Salesman</th></tr><tr><th>A</th><th>B</th><th>C</th><th>D</th></tr><tr><td>X</td><td>5</td><td>4</td><td>4</td><td>7</td></tr><tr><td>Y</td><td>7</td><td>8</td><td>5</td><td>4</td></tr><tr><td>Z</td><td>9</td><td>6</td><td>6</td><td>7</td></tr></table> | States | Salesman | | | | A | B | C | D | X | 5 | 4 | 4 | 7 | Y | 7 | 8 | 5 | 4 | Z | 9 | 6 | 6 | 7 | <p style="text-align: center;">OR</p> <p>A ready-mix plant produces concrete. Daily demand based on past data is given below</p> <table border="1"><tr><td>Daily Demand</td><td>0</td><td>15</td><td>25</td><td>35</td><td>45</td><td>50</td></tr><tr><td>Probability</td><td>0.01</td><td>0.15</td><td>0.20</td><td>0.50</td><td>0.12</td><td>0.02</td></tr></table> <p>Consider following sequence of random no. 48,78,09,51,56,77,15,14,68,09 Using the sequence</p> <ol style="list-style-type: none">1. Simulate the demand for next 10 days2. Find the stock situation of owner of the plant to make 35 kg every day. | Daily Demand | 0 | 15 | 25 | 35 | 45 | 50 | Probability | 0.01 | 0.15 | 0.20 | 0.50 | 0.12 | 0.02 | 6 | 2 | 5 | 1.1 |
|--------------|---|--|--------------------------------|----------|-------|------|-------|----|----|----|----|----|----|----|----|----|----|----|--------|----|---|---|----|----|----|---|---|--------------|---|----|----|----|----|----|-------------|------|------|-------|------|------|------|---|---|---|-----|
| | | | States | Salesman | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | A | B | C | D | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | X | 5 | 4 | 4 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | Y | 7 | 8 | 5 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Z | 9 | 6 | 6 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Daily Demand | 0 | 15 | 25 | 35 | 45 | 50 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Probability | 0.01 | 0.15 | 0.20 | 0.50 | 0.12 | 0.02 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q4(A) | Watching television also reduces the amount of physical exercise, causing weight gain. A sample of 15 10yr old children was taken. The number of pounds each child was overweight was recorded (-ve sign shows child is underweight) the no. of hours of TV viewing per week also recorded. Fit the regression line. | <table border="1"><tr><td>TV</td><td>42</td><td>34</td><td>25</td><td>35</td><td>37</td><td>38</td><td>33</td><td>33</td><td>19</td><td>29</td><td>38</td><td>28</td><td>29</td><td>36</td><td>18</td></tr><tr><td>Overwt</td><td>18</td><td>6</td><td>0</td><td>-1</td><td>13</td><td>14</td><td>7</td><td>7</td><td>-9</td><td>8</td><td>8</td><td>5</td><td>3</td><td>14</td><td>-7</td></tr></table> | TV | 42 | 34 | 25 | 35 | 37 | 38 | 33 | 33 | 19 | 29 | 38 | 28 | 29 | 36 | 18 | Overwt | 18 | 6 | 0 | -1 | 13 | 14 | 7 | 7 | -9 | 8 | 8 | 5 | 3 | 14 | -7 | 10 | 1 | 5 | 1.3.1 | | | | | | | |
| | | | TV | 42 | 34 | 25 | 35 | 37 | 38 | 33 | 33 | 19 | 29 | 38 | 28 | 29 | 36 | 18 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | Overwt | 18 | 6 | 0 | -1 | 13 | 14 | 7 | 7 | -9 | 8 | 8 | 5 | 3 | 14 | -7 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q4(B) | Using Big-M method to solve, Max $Z = 6X_1 - 3X_2 + 2X_3$ Subject to, $2X_1 + X_2 + X_3 \leq 16$ $3X_1 + 2X_2 + X_3 \leq 18$ $X_2 - 2X_3 \geq 8$ All X_1 to X_3 are equal to or greater than zero. | 10 | 3 | 3 | 1.3.2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | Q5(A) | Explain central limit theorem. | 6 | 2 | 2 | 1.3.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q5(B) | short note on Hypergeometric and Exponential distribution. | 7 | 1 | 2 | 1.3.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q5(C) | what are sampling and non-sampling errors? | 7 | 3 | 2 | 1.3.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q6(A) | A potential buyer of fluorescent lamp brought 50 lamps of each of two bands e.g. national lamp and Indian lamp. after testing lamps, he found that national had mean life of 1282 hrs with population std dev 80 hrs whereas Indian brand lamp has mean life 1208 hrs and std dev 94 hrs.at 5% can buyer conclude that both brands have same mean life? | 10 | 1 | 5 | 2.1.3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|------------|--|------------|-------------|-----|-------|--------|------|--------|------|-----|------|-----|------|---|----|---|----|---|---|---|----|---|----|----|----|---|----|---|---|---|----|----|---|--------|----|---|---|----|---|--|----|---|---|-------|
| Q6(B) | Use following data to find- 1. Fit a regression equation of Y on X and predict Y if X=8 2. Fit a regression equation of X on Y and predict X if Y=4 | 10 | 2 | 5 | 2.4.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | <table><tr><td>X</td><td>1</td><td>5</td><td>3</td><td>2</td><td>1</td><td>1</td><td>7</td><td>3</td></tr><tr><td>Y</td><td>6</td><td>1</td><td>0</td><td>0</td><td>1</td><td>2</td><td>1</td><td>5</td></tr></table> | X | 1 | 5 | 3 | 2 | 1 | 1 | 7 | 3 | Y | 6 | 1 | 0 | 0 | 1 | 2 | 1 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | |
| X | 1 | 5 | 3 | 2 | 1 | 1 | 7 | 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Y | 6 | 1 | 0 | 0 | 1 | 2 | 1 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q7(A) | Solve by Expected monetary value criteria (EMV), Expected opportunity loss (EOL) criteria. -A departmental store purchases Christmas trees which can be order in lots of 100. Each tree cost is Rs 25/- and sell cost Rs 40/- each. Unsold tresses have no salvage value. The probability distribution is given. | 10 | 2 | 4 | 2.2.4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | <table><tr><td>Trees Sold</td><td>Probability</td></tr><tr><td>100</td><td>0.20</td></tr><tr><td>200</td><td>0.35</td></tr><tr><td>300</td><td>0.25</td></tr><tr><td>400</td><td>0.15</td></tr><tr><td>500</td><td>0.05</td></tr></table> | Trees Sold | Probability | 100 | 0.20 | 200 | 0.35 | 300 | 0.25 | 400 | 0.15 | 500 | 0.05 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Trees Sold | Probability | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 100 | 0.20 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 200 | 0.35 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 300 | 0.25 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 400 | 0.15 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 500 | 0.05 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q7(B) | <table><tr><td></td><td colspan="5">Sources</td><td>Supply</td></tr><tr><td rowspan="4">Jobs</td><td>3</td><td>4</td><td>6</td><td>8</td><td>9</td><td>20</td></tr><tr><td>2</td><td>10</td><td>1</td><td>5</td><td>8</td><td>30</td></tr><tr><td>7</td><td>11</td><td>20</td><td>40</td><td>3</td><td>15</td></tr><tr><td>2</td><td>1</td><td>9</td><td>14</td><td>16</td><td>3</td></tr><tr><td>Demand</td><td>40</td><td>6</td><td>8</td><td>18</td><td>6</td><td></td></tr></table> Use following methods to find optimal transportation cost and Check optimality of solution. 1.N-W corner method 2. Least cost Method 3.VAM | | Sources | | | | | Supply | Jobs | 3 | 4 | 6 | 8 | 9 | 20 | 2 | 10 | 1 | 5 | 8 | 30 | 7 | 11 | 20 | 40 | 3 | 15 | 2 | 1 | 9 | 14 | 16 | 3 | Demand | 40 | 6 | 8 | 18 | 6 | | 10 | 3 | 5 | 2.2.4 |
| | Sources | | | | | Supply | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Jobs | 3 | 4 | 6 | 8 | 9 | 20 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 2 | 10 | 1 | 5 | 8 | 30 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 7 | 11 | 20 | 40 | 3 | 15 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 2 | 1 | 9 | 14 | 16 | 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Demand | 40 | 6 | 8 | 18 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

Table 1: Area Under Normal Curve

An entry in the table is the proportion under the entire curve which is between $z = 0$ and a positive value of z . Areas for negative values for z are obtained by symmetry.



Areas of a standard normal distribution

| z | .0 | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| .0 | .0000 | .0040 | .0080 | .0120 | .0160 | .0199 | .0239 | .0279 | .0319 | .0359 |
| .1 | .0398 | .0438 | .0478 | .0517 | .0557 | .0596 | .0636 | .0675 | .0714 | .0753 |
| .2 | .0793 | .0832 | .0871 | .0910 | .0948 | .0987 | .1026 | .1064 | .1103 | .1141 |
| .3 | .1179 | .1217 | .1255 | .1293 | .1331 | .1368 | .1406 | .1443 | .1480 | .1517 |
| .4 | .1554 | .1591 | .1628 | .1664 | .1700 | .1736 | .1772 | .1808 | .1844 | .1879 |
| .5 | .1915 | .1950 | .1985 | .2019 | .2054 | .2088 | .2123 | .2157 | .2190 | .2224 |
| .6 | .2257 | .2291 | .2324 | .2357 | .2389 | .2422 | .2454 | .2486 | .2517 | .2549 |
| .7 | .2580 | .2611 | .2642 | .2673 | .2703 | .2734 | .2764 | .2794 | .2823 | .2852 |
| .8 | .2881 | .2910 | .2939 | .2967 | .2995 | .3023 | .3051 | .3078 | .3106 | .3133 |
| .9 | .3159 | .3186 | .3212 | .3238 | .3264 | .3289 | .3315 | .3340 | .3365 | .3389 |
| 1.0 | .3413 | .3438 | .3461 | .3485 | .3508 | .3531 | .3554 | .3577 | .3599 | .3621 |
| 1.1 | .3643 | .3665 | .3686 | .3708 | .3729 | .3749 | .3770 | .3790 | .3810 | .3830 |
| 1.2 | .3849 | .3869 | .3888 | .3907 | .3925 | .3944 | .3962 | .3980 | .3997 | .4015 |
| 1.3 | .4032 | .4049 | .4066 | .4082 | .4099 | .4115 | .4131 | .4147 | .4162 | .4177 |
| 1.4 | .4192 | .4207 | .4222 | .4236 | .4251 | .4265 | .4279 | .4292 | .4306 | .4319 |
| 1.5 | .4332 | .4345 | .4357 | .4370 | .4382 | .4394 | .4406 | .4418 | .4429 | .4441 |
| 1.6 | .4452 | .4463 | .4474 | .4484 | .4495 | .4505 | .4515 | .4525 | .4535 | .4545 |
| 1.7 | .4554 | .4564 | .4573 | .4582 | .4591 | .4599 | .4608 | .4616 | .4625 | .4633 |
| 1.8 | .4641 | .4649 | .4656 | .4664 | .4671 | .4678 | .4686 | .4693 | .4699 | .4706 |
| 1.9 | .4713 | .4719 | .4726 | .4732 | .4738 | .4744 | .4750 | .4756 | .4761 | .4767 |
| 2.0 | .4772 | .4778 | .4783 | .4788 | .4793 | .4798 | .4803 | .4808 | .4812 | .4817 |
| 2.1 | .4821 | .4826 | .4830 | .4834 | .4838 | .4842 | .4846 | .4850 | .4854 | .4857 |
| 2.2 | .4861 | .4864 | .4868 | .4871 | .4875 | .4878 | .4881 | .4884 | .4887 | .4890 |
| 2.3 | .4893 | .4896 | .4898 | .4901 | .4904 | .4906 | .4909 | .4911 | .4913 | .4916 |
| 2.4 | .4918 | .4920 | .4922 | .4925 | .4927 | .4929 | .4931 | .4932 | .4934 | .4936 |
| 2.5 | .4938 | .4940 | .4941 | .4943 | .4945 | .4946 | .4948 | .4949 | .4951 | .4952 |
| 2.6 | .4953 | .4955 | .4956 | .4957 | .4959 | .4960 | .4961 | .4962 | .4963 | .4964 |
| 2.7 | .4965 | .4966 | .4967 | .4968 | .4969 | .4970 | .4971 | .4972 | .4973 | .4974 |
| 2.8 | .4974 | .4975 | .4976 | .4977 | .4977 | .4978 | .4979 | .4979 | .4980 | .4981 |
| 2.9 | .4981 | .4982 | .4982 | .4983 | .4984 | .4984 | .4985 | .4985 | .4986 | .4986 |
| 3.0 | .4987 | .4987 | .4987 | .4988 | .4988 | .4989 | .4989 | .4989 | .4990 | .4990 |

Table 2: Critical Values of Student's *t*-Distribution

| d.f. | Level of significance for two-tailed test | | | | | d.f. |
|----------|---|-------|--------|--------|--------|----------|
| | 0.20 | 0.10 | 0.05 | 0.02 | 0.01 | |
| | Level of significance for one-tailed test | | | | | |
| | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 | |
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 | 1 |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 2 |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 3 |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 4 |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 5 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 6 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 7 |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 8 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 9 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 10 |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 11 |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 12 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 13 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 14 |
| 15 | 1.341 | 1.753 | 2.731 | 2.602 | 2.947 | 15 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 16 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 17 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 18 |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 19 |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 20 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 21 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 22 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 23 |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 24 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 25 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 26 |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 27 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 28 |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 29 |
| Infinity | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 | Infinity |

Table 3: Critical Values of χ^2

| Degrees of freedom | Probability under H_0 that of $\chi^2 >$ Chi square | | | | | | |
|--------------------|---|--------|--------|--------|--------|--------|--------|
| | .99 | .95 | .50 | .10 | .05 | .02 | .01 |
| 1 | .000157 | .00393 | .455 | 2.706 | 3.841 | 5.412 | 6.635 |
| 2 | .0201 | .103 | 1.386 | 4.605 | 5.991 | 7.824 | 9.210 |
| 3 | .115 | .352 | 2.366 | 6.251 | 7.815 | 9.837 | 11.341 |
| 4 | .297 | .711 | 3.357 | 7.779 | 9.488 | 11.668 | 13.277 |
| 5 | .554 | 1.145 | 4.351 | 9.236 | 11.070 | 13.388 | 15.086 |
| 6 | .872 | 1.635 | 5.348 | 10.645 | 12.592 | 15.033 | 16.812 |
| 7 | 1.239 | 2.167 | 6.346 | 12.017 | 14.067 | 16.622 | 18.475 |
| 8 | 1.646 | 2.733 | 7.344 | 13.362 | 15.507 | 18.168 | 20.090 |
| 9 | 2.088 | 3.325 | 8.343 | 14.684 | 16.919 | 19.679 | 21.666 |
| 10 | 2.558 | 3.940 | 9.342 | 15.987 | 18.307 | 21.161 | 23.209 |
| 11 | 3.053 | 4.575 | 10.341 | 17.275 | 19.675 | 22.618 | 24.725 |
| 12 | 3.571 | 5.226 | 11.340 | 18.549 | 21.026 | 24.054 | 26.217 |
| 13 | 4.107 | 5.892 | 12.340 | 19.812 | 22.362 | 25.472 | 27.688 |
| 14 | 4.660 | 6.571 | 13.339 | 21.064 | 23.685 | 26.873 | 29.141 |
| 15 | 4.229 | 7.261 | 14.339 | 22.307 | 24.996 | 28.259 | 30.578 |
| 16 | 5.812 | 7.962 | 15.338 | 23.542 | 26.296 | 29.633 | 32.000 |
| 17 | 6.408 | 8.672 | 16.338 | 24.769 | 27.587 | 30.995 | 33.409 |
| 18 | 7.015 | 9.390 | 17.338 | 25.989 | 28.869 | 32.346 | 34.805 |
| 19 | 7.633 | 10.117 | 18.338 | 27.204 | 30.144 | 33.687 | 36.191 |
| 20 | 8.260 | 10.851 | 19.337 | 28.412 | 31.410 | 35.020 | 37.566 |
| 21 | 8.897 | 11.591 | 20.337 | 29.615 | 32.671 | 36.343 | 38.932 |
| 22 | 9.542 | 12.338 | 21.337 | 30.813 | 33.924 | 37.659 | 40.289 |
| 23 | 10.196 | 13.091 | 22.337 | 32.007 | 35.172 | 38.968 | 41.638 |
| 24 | 10.856 | 13.848 | 23.337 | 32.196 | 36.415 | 40.270 | 42.980 |
| 25 | 11.524 | 14.611 | 24.337 | 34.382 | 37.652 | 41.566 | 44.314 |
| 26 | 12.198 | 15.379 | 25.336 | 35.363 | 38.885 | 41.856 | 45.642 |
| 27 | 12.879 | 16.151 | 26.336 | 36.741 | 40.113 | 44.140 | 46.963 |
| 28 | 13.565 | 16.928 | 27.336 | 37.916 | 41.337 | 45.419 | 48.278 |
| 29 | 14.256 | 17.708 | 28.336 | 39.087 | 42.557 | 46.693 | 49.588 |
| 30 | 14.953 | 18.493 | 29.336 | 40.256 | 43.773 | 47.962 | 50.892 |

Note: For degrees of freedom greater than 30, the quantity $2\chi^2 - \sqrt{2d.f. - 1}$ may be used as a normal variate with unit variance i.e., $z_\alpha = \sqrt{2\chi^2} - \sqrt{2d.f. - 1}$.

Table 4(a): Critical Values of *F*-Distribution (at 5 per cent)

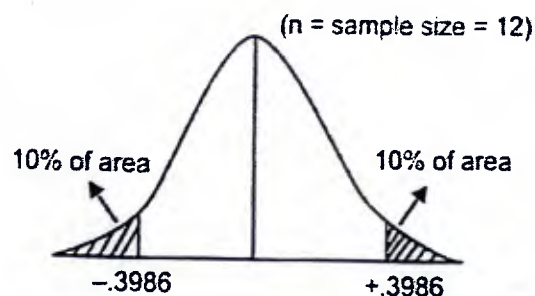
| $v_1 \backslash v_2$ | 1 | 2 | 3 | 4 | 5 | 6 | 8 | 12 | 24 | ∞ |
|----------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1 | 161.4 | 199.5 | 215.7 | 224.6 | 230.2 | 234.0 | 238.9 | 243.9 | 249.1 | 243.3 |
| 2 | 18.51 | 19.00 | 19.16 | 19.25 | 19.30 | 19.33 | 19.37 | 19.41 | 19.45 | 19.50 |
| 3 | 10.13 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.85 | 8.74 | 8.64 | 8.53 |
| 4 | 7.71 | 6.94 | 6.59 | 6.39 | 6.26 | 6.16 | 6.04 | 5.91 | 5.77 | 5.63 |
| 5 | 6.61 | 5.79 | 5.41 | 5.19 | 5.05 | 4.95 | 4.82 | 4.68 | 4.53 | 4.36 |
| 6 | 5.99 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.15 | 4.00 | 3.84 | 3.67 |
| 7 | 5.59 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.73 | 3.57 | 3.41 | 3.23 |
| 8 | 5.32 | 4.46 | 4.07 | 3.84 | 3.69 | 3.58 | 3.44 | 3.28 | 3.12 | 2.93 |
| 9 | 5.12 | 4.26 | 3.86 | 3.63 | 3.48 | 3.37 | 3.23 | 3.07 | 2.90 | 2.71 |
| 10 | 4.96 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.07 | 2.91 | 2.74 | 2.54 |
| 11 | 4.84 | 3.98 | 3.59 | 3.36 | 3.20 | 3.09 | 2.95 | 2.79 | 2.61 | 2.40 |
| 12 | 4.75 | 3.88 | 3.49 | 3.26 | 3.11 | 3.00 | 2.85 | 2.69 | 2.51 | 2.30 |
| 13 | 4.67 | 3.80 | 3.41 | 3.18 | 3.02 | 2.92 | 2.77 | 2.60 | 2.42 | 2.21 |
| 14 | 4.60 | 3.74 | 3.34 | 3.11 | 2.96 | 2.85 | 2.70 | 2.53 | 2.35 | 2.13 |
| 15 | 4.54 | 3.68 | 3.29 | 3.06 | 2.90 | 2.79 | 2.64 | 2.48 | 2.29 | 2.07 |
| 16 | 4.49 | 3.63 | 3.24 | 3.01 | 2.85 | 2.74 | 2.59 | 2.42 | 2.24 | 2.01 |
| 17 | 4.45 | 3.59 | 3.20 | 2.96 | 2.81 | 2.70 | 2.55 | 2.38 | 2.19 | 1.96 |
| 18 | 4.41 | 3.55 | 3.16 | 2.93 | 2.77 | 2.66 | 2.51 | 2.34 | 2.15 | 1.92 |
| 19 | 4.38 | 3.52 | 3.13 | 2.90 | 2.74 | 2.63 | 2.48 | 2.31 | 2.11 | 1.88 |
| 20 | 4.35 | 3.49 | 3.10 | 2.87 | 2.71 | 2.60 | 2.45 | 2.28 | 2.08 | 1.84 |
| 21 | 4.32 | 3.47 | 3.07 | 2.84 | 2.68 | 2.57 | 2.42 | 2.25 | 2.05 | 1.81 |
| 22 | 4.30 | 3.44 | 3.05 | 2.82 | 2.66 | 2.55 | 2.40 | 2.23 | 2.03 | 1.78 |
| 23 | 4.28 | 3.42 | 3.03 | 2.80 | 2.64 | 2.53 | 2.38 | 2.20 | 2.01 | 1.76 |
| 24 | 4.26 | 3.40 | 3.01 | 2.78 | 2.62 | 2.51 | 2.36 | 2.18 | 1.98 | 1.73 |
| 25 | 4.24 | 3.38 | 2.99 | 2.76 | 2.60 | 2.49 | 2.34 | 2.16 | 1.96 | 1.71 |
| 26 | 4.22 | 3.37 | 2.98 | 2.74 | 2.59 | 2.47 | 2.32 | 2.15 | 1.95 | 1.69 |
| 27 | 4.21 | 3.35 | 2.96 | 2.73 | 2.57 | 2.46 | 2.31 | 2.13 | 1.93 | 1.67 |
| 28 | 4.20 | 3.34 | 2.95 | 2.71 | 2.56 | 2.45 | 2.29 | 2.12 | 1.91 | 1.65 |
| 29 | 4.18 | 3.33 | 2.93 | 2.70 | 2.54 | 2.43 | 2.28 | 2.10 | 1.90 | 1.64 |
| 30 | 4.17 | 3.32 | 2.92 | 2.69 | 2.53 | 2.42 | 2.27 | 2.09 | 1.89 | 1.62 |
| 40 | 4.08 | 3.23 | 2.84 | 2.61 | 2.45 | 2.34 | 2.18 | 2.00 | 1.79 | 1.51 |
| 60 | 4.00 | 3.15 | 2.76 | 2.52 | 2.37 | 2.25 | 2.10 | 1.92 | 1.70 | 1.39 |
| 120 | 3.92 | 3.07 | 2.68 | 2.45 | 2.29 | 2.17 | 2.02 | 1.83 | 1.61 | 1.25 |
| ∞ | 3.84 | 2.99 | 2.60 | 2.37 | 2.21 | 2.10 | 1.94 | 1.75 | 1.52 | 1.00 |

v_1 = Degrees of freedom for greater variance.
 v_2 = Degrees of freedom for smaller variance.

Table 4(b): Critical Values of *F*-Distribution (at 1 per cent)

| $v_1 \backslash v_2$ | 1 | 2 | 3 | 4 | 5 | 6 | 8 | 12 | 24 | ∞ |
|----------------------|-------|--------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1 | 4052 | 4999.5 | 5403 | 5625 | 5764 | 5859 | 5982 | 6106 | 6235 | 6366 |
| 2 | 98.50 | 99.00 | 99.17 | 99.25 | 99.30 | 99.33 | 99.37 | 99.42 | 99.46 | 99.50 |
| 3 | 34.12 | 30.82 | 29.46 | 28.71 | 28.24 | 27.91 | 27.49 | 27.05 | 26.60 | 26.13 |
| 4 | 21.20 | 18.00 | 16.69 | 15.98 | 15.52 | 15.21 | 14.80 | 14.37 | 13.93 | 13.45 |
| 5 | 16.26 | 13.27 | 12.06 | 11.39 | 10.97 | 10.67 | 10.29 | 9.89 | 9.47 | 9.02 |
| 6 | 13.75 | 10.92 | 9.78 | 9.15 | 8.75 | 8.47 | 8.10 | 7.72 | 7.31 | 6.88 |
| 7 | 12.25 | 9.55 | 8.45 | 7.85 | 7.46 | 7.19 | 6.84 | 6.47 | 6.07 | 5.65 |
| 8 | 11.26 | 8.65 | 7.59 | 7.01 | 6.63 | 6.37 | 6.03 | 5.67 | 5.28 | 4.86 |
| 9 | 10.56 | 8.02 | 6.99 | 6.42 | 6.06 | 5.80 | 5.47 | 5.11 | 4.73 | 4.31 |
| 10 | 10.04 | 7.56 | 6.55 | 5.99 | 5.64 | 5.39 | 5.06 | 4.71 | 4.33 | 3.91 |
| 11 | 9.65 | 7.21 | 6.22 | 5.87 | 5.52 | 5.07 | 4.74 | 4.40 | 4.02 | 3.60 |
| 12 | 9.33 | 6.93 | 5.95 | 5.41 | 5.06 | 4.82 | 4.50 | 4.16 | 3.78 | 3.36 |
| 13 | 9.07 | 6.70 | 5.74 | 5.21 | 4.86 | 4.62 | 4.30 | 3.96 | 3.59 | 3.17 |
| 14 | 8.86 | 6.51 | 5.56 | 5.04 | 4.69 | 4.46 | 4.14 | 3.80 | 3.43 | 3.00 |
| 15 | 8.68 | 6.36 | 5.42 | 4.89 | 4.56 | 4.32 | 4.00 | 3.67 | 3.29 | 2.87 |
| 16 | 8.53 | 6.23 | 5.29 | 4.77 | 4.44 | 4.20 | 3.89 | 3.55 | 3.18 | 2.75 |
| 17 | 8.40 | 6.11 | 5.18 | 4.67 | 4.34 | 4.10 | 3.79 | 3.46 | 3.08 | 2.65 |
| 18 | 8.29 | 6.01 | 5.09 | 4.58 | 4.25 | 4.01 | 3.71 | 3.37 | 3.00 | 2.57 |
| 19 | 8.18 | 5.93 | 5.01 | 4.50 | 4.17 | 3.94 | 3.63 | 3.30 | 2.92 | 2.49 |
| 20 | 8.10 | 5.85 | 4.94 | 4.43 | 4.10 | 3.87 | 3.56 | 3.23 | 2.86 | 2.42 |
| 21 | 8.02 | 5.78 | 4.87 | 4.37 | 4.04 | 3.81 | 3.51 | 3.17 | 2.80 | 2.36 |
| 22 | 7.95 | 5.72 | 4.82 | 4.31 | 3.99 | 3.76 | 3.45 | 3.12 | 2.75 | 2.31 |
| 23 | 7.88 | 5.66 | 4.76 | 4.26 | 3.94 | 3.71 | 3.41 | 3.07 | 2.70 | 2.26 |
| 24 | 7.82 | 5.61 | 4.72 | 4.22 | 3.90 | 3.67 | 3.36 | 3.03 | 2.66 | 2.21 |
| 25 | 7.77 | 5.57 | 4.68 | 4.18 | 3.85 | 3.63 | 3.32 | 2.99 | 2.62 | 2.17 |
| 26 | 7.72 | 5.53 | 4.64 | 4.14 | 3.82 | 3.59 | 3.20 | 2.96 | 2.58 | 2.10 |
| 27 | 7.68 | 5.49 | 4.60 | 4.11 | 3.78 | 3.56 | 3.26 | 2.93 | 2.45 | 2.13 |
| 28 | 7.64 | 5.45 | 4.57 | 4.07 | 3.75 | 3.53 | 3.23 | 2.90 | 2.52 | 2.06 |
| 29 | 7.60 | 5.42 | 4.54 | 4.04 | 3.73 | 3.50 | 3.20 | 2.87 | 2.49 | 2.03 |
| 30 | 7.56 | 5.39 | 4.51 | 4.02 | 3.70 | 3.47 | 3.17 | 2.84 | 2.47 | 2.01 |
| 40 | 7.31 | 5.18 | 4.31 | 3.83 | 3.51 | 3.29 | 2.99 | 2.66 | 2.29 | 1.80 |
| 60 | 7.08 | 4.98 | 4.13 | 3.65 | 3.34 | 3.12 | 2.82 | 2.50 | 2.12 | 1.60 |
| 120 | 6.85 | 4.79 | 3.95 | 3.48 | 3.17 | 2.96 | 2.66 | 2.34 | 1.95 | 1.38 |
| ∞ | 6.64 | 4.60 | 3.78 | 3.32 | 3.02 | 2.80 | 2.51 | 2.18 | 1.79 | 1.00 |

 v_1 = Degrees of freedom for greater variance. v_2 = Degrees of freedom for smaller variance.

Table 5: Values for Spearman's Rank Correlation (r) for Combined Areas in Both Tails

| n | .20 | .10 | .05 | .02 | .01 | .002 |
|-----|-------|-------|-------|-------|-------|-------|
| 4 | .8000 | .8000 | — | — | — | — |
| 5 | .7000 | .8000 | .9000 | .9000 | — | — |
| 6 | .6000 | .7714 | .8236 | .8857 | .9429 | — |
| 7 | .5357 | .6786 | .7450 | .8571 | .8929 | .9643 |
| 8 | .5000 | .6190 | .7143 | .8095 | .8571 | .9286 |
| 9 | .4667 | .5833 | .6833 | .7667 | .8167 | .9000 |
| 10 | .4424 | .5515 | .6364 | .7333 | .7818 | .8667 |
| 11 | .4182 | .5273 | .6091 | .7000 | .7455 | .8364 |
| 12 | .3986 | .4965 | .5804 | .6713 | .7273 | .8182 |
| 13 | .3791 | .4780 | .5549 | .6429 | .6978 | .7912 |
| 14 | .3626 | .4593 | .5341 | .6220 | .6747 | .7670 |
| 15 | .3500 | .4429 | .5179 | .6000 | .6536 | .7464 |
| 16 | .3382 | .4265 | .5000 | .5824 | .6324 | .7265 |
| 17 | .3260 | .4118 | .4853 | .5637 | .6152 | .7083 |
| 18 | .3148 | .3994 | .4716 | .5480 | .5975 | .6904 |
| 19 | .3070 | .3895 | .4579 | .5333 | .5825 | .6737 |
| 20 | .2977 | .3789 | .4451 | .5203 | .5684 | .6586 |
| 21 | .2909 | .3688 | .4351 | .5078 | .5545 | .6455 |
| 22 | .2829 | .3597 | .4241 | .4963 | .5426 | .6318 |
| 23 | .2767 | .3518 | .4150 | .4852 | .5306 | .6186 |
| 24 | .2704 | .3435 | .4061 | .4748 | .5200 | .6070 |
| 25 | .2646 | .3362 | .3977 | .4654 | .5100 | .5962 |
| 26 | .2588 | .3299 | .3894 | .4564 | .5002 | .5856 |
| 27 | .2540 | .3236 | .3822 | .4481 | .4915 | .5757 |
| 28 | .2480 | .3175 | .3749 | .4401 | .4828 | .5660 |
| 29 | .2443 | .3113 | .3685 | .4320 | .4744 | .5567 |
| 30 | .2400 | .3059 | .3620 | .4251 | .4665 | .5479 |

| cum. prob | t _{.50} | t _{.75} | t _{.80} | t _{.90} | t _{.95} | t _{.975} | t _{.99} | t _{.995} |
|-----------|------------------|------------------|------------------|------------------|------------------|-------------------|------------------|-------------------|
| one-tail | 0.50 | 0.25 | 0.20 | 0.15 | 0.10 | 0.05 | 0.01 | 0.0005 |
| two-tails | 1.00 | 0.50 | 0.40 | 0.30 | 0.20 | 0.10 | 0.02 | 0.001 |
| df | | | | | | | | |
| 1 | 0.000 | 1.000 | 1.376 | 1.883 | 3.078 | 6.314 | 31.82 | 636.62 |
| 2 | 0.000 | 0.816 | 1.081 | 1.386 | 1.886 | 2.920 | 6.965 | 31.599 |
| 3 | 0.000 | 0.765 | 0.978 | 1.250 | 1.638 | 2.353 | 4.541 | 12.924 |
| 4 | 0.000 | 0.741 | 0.941 | 1.190 | 1.533 | 2.132 | 3.747 | 8.610 |
| 5 | 0.000 | 0.727 | 0.920 | 1.158 | 1.476 | 2.015 | 3.365 | 6.869 |
| 6 | 0.000 | 0.715 | 0.908 | 1.134 | 1.440 | 1.943 | 3.143 | 5.959 |
| 7 | 0.000 | 0.711 | 0.896 | 1.119 | 1.415 | 1.895 | 2.998 | 5.408 |
| 8 | 0.000 | 0.706 | 0.889 | 1.108 | 1.397 | 1.860 | 2.896 | 5.041 |
| 9 | 0.000 | 0.703 | 0.883 | 1.100 | 1.383 | 1.833 | 2.821 | 4.781 |
| 10 | 0.000 | 0.700 | 0.879 | 1.093 | 1.372 | 1.812 | 2.764 | 4.587 |
| 11 | 0.000 | 0.697 | 0.876 | 1.088 | 1.363 | 1.796 | 2.718 | 4.437 |
| 12 | 0.000 | 0.695 | 0.873 | 1.083 | 1.356 | 1.782 | 2.681 | 4.318 |
| 13 | 0.000 | 0.694 | 0.870 | 1.079 | 1.350 | 1.771 | 2.650 | 4.221 |
| 14 | 0.000 | 0.692 | 0.868 | 1.076 | 1.345 | 1.761 | 2.624 | 4.140 |
| 15 | 0.000 | 0.691 | 0.866 | 1.074 | 1.341 | 1.753 | 2.602 | 4.073 |
| 16 | 0.000 | 0.690 | 0.865 | 1.071 | 1.337 | 1.746 | 2.583 | 4.015 |
| 17 | 0.000 | 0.689 | 0.863 | 1.069 | 1.333 | 1.740 | 2.567 | 3.965 |
| 18 | 0.000 | 0.688 | 0.862 | 1.067 | 1.330 | 1.734 | 2.552 | 3.922 |
| 19 | 0.000 | 0.688 | 0.861 | 1.066 | 1.328 | 1.729 | 2.539 | 3.883 |
| 20 | 0.000 | 0.687 | 0.860 | 1.064 | 1.325 | 1.725 | 2.528 | 3.850 |
| 21 | 0.000 | 0.686 | 0.859 | 1.063 | 1.323 | 1.721 | 2.518 | 3.819 |
| 22 | 0.000 | 0.686 | 0.858 | 1.061 | 1.321 | 1.717 | 2.508 | 3.792 |
| 23 | 0.000 | 0.685 | 0.858 | 1.060 | 1.319 | 1.714 | 2.500 | 3.768 |
| 24 | 0.000 | 0.685 | 0.857 | 1.059 | 1.318 | 1.711 | 2.492 | 3.745 |
| 25 | 0.000 | 0.684 | 0.856 | 1.058 | 1.316 | 1.708 | 2.485 | 3.725 |
| 26 | 0.000 | 0.684 | 0.856 | 1.058 | 1.315 | 1.706 | 2.479 | 3.707 |
| 27 | 0.000 | 0.684 | 0.855 | 1.057 | 1.314 | 1.703 | 2.473 | 3.690 |
| 28 | 0.000 | 0.683 | 0.855 | 1.056 | 1.313 | 1.701 | 2.467 | 3.674 |
| 29 | 0.000 | 0.683 | 0.854 | 1.055 | 1.311 | 1.698 | 2.462 | 3.659 |
| 30 | 0.000 | 0.683 | 0.854 | 1.055 | 1.310 | 1.697 | 2.457 | 3.646 |
| 40 | 0.000 | 0.681 | 0.851 | 1.050 | 1.303 | 1.684 | 2.423 | 3.551 |
| 60 | 0.000 | 0.679 | 0.848 | 1.045 | 1.296 | 1.671 | 2.390 | 3.460 |
| 80 | 0.000 | 0.678 | 0.846 | 1.043 | 1.292 | 1.664 | 2.374 | 3.416 |
| 100 | 0.000 | 0.677 | 0.845 | 1.042 | 1.290 | 1.660 | 2.364 | 3.390 |
| 1000 | 0.000 | 0.676 | 0.842 | 1.037 | 1.282 | 1.646 | 2.330 | 3.300 |
| Z | 0.000 | 0.674 | 0.842 | 1.036 | 1.282 | 1.645 | 2.326 | 3.291 |
| | 0% | 50% | 60% | 70% | 80% | 90% | 98% | 99.9% |



Bharatiya Vidya Bhavan's

Sardar Patel College of Engineering

(A Government Aided Autonomous Institute)

Munshi Nagar, Andheri (West), Mumbai – 400058.

ReExaminations, July 2022

A. Y. M. Patel (Contn. mg) *Sum I*



Total points: 100

Duration: Total Time allotted will be 3Hr.

Class: M.TECH(CM).

Semester: I

Program: Civil

Name of the Course: Applied Statistics and Quantitative Techniques Course Code : PC-MTCM-102

Instructions:

1. All Questions are compulsory
2. Draw neat diagrams
3. Assume suitable data if necessary and state the clearly.

1817/22

| Que. No | | Points | CO | BL | PI | | | | | | | | | | | | | | | | |
|--------------|--|---------|--------|---------|-------|--------------|----|----|----|-----------|-----|-----|-----|-------|-----|-----|-----|----|-----|---|-------|
| Q1(a) | <p>1.1 A random sample of size 10 from a normal population gives a sample mean of 22 and sample SD 6. Test if the population mean is 24?</p> <p>1.2 The mean lifetime of 30 fans produced by a company is computed to be 1500 hours with SD 100 hrs. The company claims that the average life of fans produced by them is 1650 hours. Is the claim acceptable.</p> <p>1.3 if a 5% of items produced turn out to be defective then find out probability that out of 20 items selected at random there are using binomial Distribution-</p> <p>1. exactly three defectives</p> <p>2. At least two defectives</p> <p>3. find mean and variance</p> | 10 | 1,2 | 3 | 1.2.3 | | | | | | | | | | | | | | | | |
| Q1(b) | <p>1.1 The side effects of a new drug are being tested against a placebo. A simple random sample of 565 patients yields the results below. At a significance level of $\alpha= 0:05$, is there enough evidence to conclude that the treatment is independent of the side effect of nausea?</p> <table border="1"><tr><td>result</td><td>Drug 1</td><td>Placebo</td><td>Total</td></tr><tr><td>Nausea (r.1)</td><td>36</td><td>13</td><td>49</td></tr><tr><td>No Nausea</td><td>254</td><td>262</td><td>515</td></tr><tr><td>Total</td><td>290</td><td>275</td><td>565</td></tr></table> <p>1.2 Explain normal Distribution and its characteristics</p> <p>1.3 a small scale unit operates an automatic machine which produces screws . it is know from past records that machine produces 5% defective on an average. Certain unassembled screws needs 95 such screws for assembly and is supplied with a box of 100 screws produced by the unit. what is probability that purchase of a box(using Possions Distribution)-</p> <p>1. will get exactly five defectives I the box</p> <p>2. will not have enough screws to complete assembly</p> | result | Drug 1 | Placebo | Total | Nausea (r.1) | 36 | 13 | 49 | No Nausea | 254 | 262 | 515 | Total | 290 | 275 | 565 | 10 | 2,3 | 3 | 1.2.3 |
| result | Drug 1 | Placebo | Total | | | | | | | | | | | | | | | | | | |
| Nausea (r.1) | 36 | 13 | 49 | | | | | | | | | | | | | | | | | | |
| No Nausea | 254 | 262 | 515 | | | | | | | | | | | | | | | | | | |
| Total | 290 | 275 | 565 | | | | | | | | | | | | | | | | | | |
| Q2(a) | <p>solve by Big-M method-</p> <p>Maximize $U= y_1+2y_2+3y_3-y_4$</p> | 10 | 3,2 | 4 | 2.2.1 | | | | | | | | | | | | | | | | |

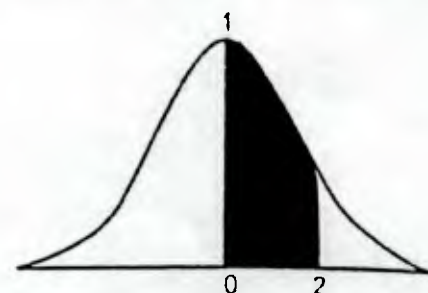
| | subject to constraints, $y_1+2y_2+3y_3=15$ $2y_1+y_2+5y_3=20$ $y_1+2y_2+y_3+y_4=10$ All y_1, \dots, y_4 greater than or equal to 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|------------------|---|-----------------|--|---|---|--|---|----|-----|-------|----|----|------|-----------------|---|----|------|------------------|----|----|-----|-----------------|--------|--------|----|---------|-------------|---|-------|---|------|---|------|---|------|---|------|----|-----|---|-------|
| Q2(b) | Show that there is unbounded solution to following LPP problem using Simplex method- Maximize $Z= 4y_1+y_2+3y_3+5y_4$ subject to constraints, $4y_1-6y_2-5y_3-4y_4\geq -20$ $-3y_1-2y_2+4y_3+y_4\leq 10$ $-8y_1-3y_2+3y_3+2y_4\leq 20$ $y_1, \dots, y_4 \geq 0$ | 10 | 3,2 | 4 | 2.3.2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q3(a) | 3.1 Formulate LPP and solve by Graphical Method- A firm uses lathes ,milling machines and grinding machines to produce two machine parts. Following table shows machining time required for each part, the machining times available on different machines and profit on each machine part. find the number of parts I and II to be manufactured per week to maximize the profit. <table border="1"><thead><tr><th>Type of Machine</th><th colspan="2">machining time required for each part(mints)</th><th>Maximum time available per week (Mints)</th></tr><tr><th></th><th>I</th><th>II</th><th></th></tr></thead><tbody><tr><td>Lathe</td><td>12</td><td>6</td><td>3000</td></tr><tr><td>Milling machine</td><td>4</td><td>10</td><td>2000</td></tr><tr><td>Grinding machine</td><td>2</td><td>3</td><td>900</td></tr><tr><td>Profit per unit</td><td>Rs. 40</td><td>Rs.100</td><td></td></tr></tbody></table> | Type of Machine | machining time required for each part(mints) | | Maximum time available per week (Mints) | | I | II | | Lathe | 12 | 6 | 3000 | Milling machine | 4 | 10 | 2000 | Grinding machine | 2 | 3 | 900 | Profit per unit | Rs. 40 | Rs.100 | | 10 | 3,2 | 4 | 2.3.2 | | | | | | | | | | | | |
| Type of Machine | machining time required for each part(mints) | | Maximum time available per week (Mints) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | I | II | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Lathe | 12 | 6 | 3000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Milling machine | 4 | 10 | 2000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Grinding machine | 2 | 3 | 900 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Profit per unit | Rs. 40 | Rs.100 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q3(b) | 3.1 A departmental lead has three subordinates and four tasks for completion. The employees differ in their capabilities and task differ in their work content, with performance matrix given below, which three of four tasks should be assigned to the subordinates? <table border="1"><thead><tr><th>Tasks</th><th colspan="3">Subordinates</th></tr><tr><th></th><th>I</th><th>II</th><th>III</th></tr></thead><tbody><tr><td>A</td><td>9</td><td>12</td><td>11</td></tr><tr><td>B</td><td>8</td><td>13</td><td>17</td></tr><tr><td>C</td><td>20</td><td>12</td><td>13</td></tr><tr><td>D</td><td>21</td><td>15</td><td>17</td></tr></tbody></table> 3.2 A company is making a large boiler installation. A certain automatic monitoring unit is critical for operation of whole system. At the time of original order, the spares for this unit can be purchased for Rs. 2000 per unit. The probability distribution for the failure of this unit during the lifetime of installation is given by – <table border="1"><thead><tr><th>Failure</th><th>Probability</th></tr></thead><tbody><tr><td>0</td><td>0.35</td></tr><tr><td>1</td><td>0.25</td></tr><tr><td>2</td><td>0.20</td></tr><tr><td>3</td><td>0.15</td></tr><tr><td>4</td><td>0.05</td></tr></tbody></table> | Tasks | Subordinates | | | | I | II | III | A | 9 | 12 | 11 | B | 8 | 13 | 17 | C | 20 | 12 | 13 | D | 21 | 15 | 17 | Failure | Probability | 0 | 0.35 | 1 | 0.25 | 2 | 0.20 | 3 | 0.15 | 4 | 0.05 | 10 | 1,2 | 4 | 2.3.2 |
| Tasks | Subordinates | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | I | II | III | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A | 9 | 12 | 11 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | 8 | 13 | 17 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| C | 20 | 12 | 13 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| D | 21 | 15 | 17 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Failure | Probability | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0.35 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 0.25 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | 0.20 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | 0.15 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | 0.05 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|--------------------|---|--------------------|-------------|-----|-------|--------|------|--------|------|-----|------|-----|------|-----|------|-----|------|--------|----|----|-------|----|----|----|----|----|----|----|----|----|----|----|-----|--------|-------|---|-------|----|---|--|----|-----|---|-------|
| | If spare is needed and not available, the total cost of idle time and replacement cost will be Rs. 15000. Unused spares no salvage value. Determine the optimal number of spares to be ordered. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q4(a) | Weekly demand of a product is assumed to be normally distributed. Use goodness of fit and following data to test this assumption. Use alpha=0.10, sample mean=24.5 sample std dev=3 <table><tr><td>18</td><td>20</td><td>22</td><td>27</td><td>22</td><td>26</td><td>25</td><td>25</td><td>27</td><td>25</td></tr><tr><td>25</td><td>22</td><td>27</td><td>25</td><td>24</td><td>25</td><td>28</td><td>24</td><td>25</td><td>26</td></tr><tr><td>26</td><td>23</td><td>20</td><td>24</td><td>26</td><td>31</td><td>29</td><td>28</td><td>19</td><td>21</td></tr></table> | 18 | 20 | 22 | 27 | 22 | 26 | 25 | 25 | 27 | 25 | 25 | 22 | 27 | 25 | 24 | 25 | 28 | 24 | 25 | 26 | 26 | 23 | 20 | 24 | 26 | 31 | 29 | 28 | 19 | 21 | 10 | 1,2 | 2 | 1.3.2 | | | | | | | | | |
| 18 | 20 | 22 | 27 | 22 | 26 | 25 | 25 | 27 | 25 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 25 | 22 | 27 | 25 | 24 | 25 | 28 | 24 | 25 | 26 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 26 | 23 | 20 | 24 | 26 | 31 | 29 | 28 | 19 | 21 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q4(b) | Watching television also reduces the amount of physical exercise, causing weight gain. A sample of 15 10yr old children was taken. The number of pounds each child was overweight was recorded (-ve sign shows child is underweight) the no. of hours of TV viewing per week also recorded. Fit the regression line. <table><tr><td>TV</td><td>42</td><td>34</td><td>25</td><td>35</td><td>37</td><td>38</td><td>33</td><td>33</td><td>19</td><td>29</td><td>38</td><td>28</td><td>29</td><td>36</td><td>18</td></tr><tr><td>Overwt</td><td>18</td><td>6</td><td>0</td><td>-1</td><td>13</td><td>14</td><td>7</td><td>7</td><td>-9</td><td>8</td><td>8</td><td>5</td><td>3</td><td>14</td><td>-7</td></tr></table> | TV | 42 | 34 | 25 | 35 | 37 | 38 | 33 | 33 | 19 | 29 | 38 | 28 | 29 | 36 | 18 | Overwt | 18 | 6 | 0 | -1 | 13 | 14 | 7 | 7 | -9 | 8 | 8 | 5 | 3 | 14 | -7 | 10 | 1,2 | 4 | 2.3.2 | | | | | | | |
| TV | 42 | 34 | 25 | 35 | 37 | 38 | 33 | 33 | 19 | 29 | 38 | 28 | 29 | 36 | 18 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Overwt | 18 | 6 | 0 | -1 | 13 | 14 | 7 | 7 | -9 | 8 | 8 | 5 | 3 | 14 | -7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q5(a) | Explain Assignment Model? Explain central limit theorem | 10 | 3,2 | 2 | 1.3.2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q5(b) | short note on Hypergeometric and Exponential distribution. what are sampling and non-sampling errors? | 10 | 3,2 | 2 | 1.3.2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q6 | <table><tr><td></td><td colspan="5">Sources</td><td>Supply</td></tr><tr><td rowspan="4">Jobs</td><td>3</td><td>4</td><td>6</td><td>8</td><td>9</td><td>20</td></tr><tr><td>2</td><td>10</td><td>1</td><td>5</td><td>8</td><td>30</td></tr><tr><td>7</td><td>11</td><td>20</td><td>40</td><td>3</td><td>15</td></tr><tr><td>2</td><td>1</td><td>9</td><td>14</td><td>16</td><td>3</td></tr><tr><td>Demand</td><td>40</td><td>6</td><td>8</td><td>18</td><td>6</td><td></td></tr></table> Use following methods to find optimal transportation cost and Check optimality of solution. 1.N-W corner method 2. Least cost Method 3.VAM | | Sources | | | | | Supply | Jobs | 3 | 4 | 6 | 8 | 9 | 20 | 2 | 10 | 1 | 5 | 8 | 30 | 7 | 11 | 20 | 40 | 3 | 15 | 2 | 1 | 9 | 14 | 16 | 3 | Demand | 40 | 6 | 8 | 18 | 6 | | 20 | 1,2 | 3 | 2.3.2 |
| | Sources | | | | | Supply | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Jobs | 3 | 4 | 6 | 8 | 9 | 20 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 2 | 10 | 1 | 5 | 8 | 30 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 7 | 11 | 20 | 40 | 3 | 15 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 2 | 1 | 9 | 14 | 16 | 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Demand | 40 | 6 | 8 | 18 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q7(a) | 7.1An automobile company manufactures around 150 scooters. The daily production varies from 146 to 154 depending upon availability of raw material and other working conditions. <table><tr><td>Production per day</td><td>Probability</td></tr><tr><td>146</td><td>0.04</td></tr><tr><td>147</td><td>0.09</td></tr><tr><td>148</td><td>0.12</td></tr><tr><td>149</td><td>0.14</td></tr><tr><td>150</td><td>0.11</td></tr><tr><td>151</td><td>0.10</td></tr><tr><td>152</td><td>0.20</td></tr></table> | Production per day | Probability | 146 | 0.04 | 147 | 0.09 | 148 | 0.12 | 149 | 0.14 | 150 | 0.11 | 151 | 0.10 | 152 | 0.20 | 10 | 2 | 4 | 2.3.2 | | | | | | | | | | | | | | | | | | | | | | | |
| Production per day | Probability | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 146 | 0.04 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 147 | 0.09 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 148 | 0.12 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 149 | 0.14 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 150 | 0.11 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 151 | 0.10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 152 | 0.20 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

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|-------------|--|-------------|---------------|------|------|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|----|-----|---|-------|
| | <table><tr><td>153</td><td>0.12</td></tr><tr><td>154</td><td>0.08</td></tr></table> <p>The finished scooters are transported in a special truck accommodating 150 scooters. Use following random numbers- 80,81,76,75,64,43,18,26,10,12,65,68,69,61,57.</p> <p>Simulate-</p> <p>What will be average no of scooters waiting in factory?</p> <p>What will be average number of empty space on the lorry?</p> | 153 | 0.12 | 154 | 0.08 | | | | | | | | | | | | | | | | | | | | | | |
| 153 | 0.12 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 154 | 0.08 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q7(b) | <p>7.1 F-ollowing data relate to average monthly price (X) and demand(Y) of a commodity during last ten months. determine the Karl Pearson's correlation coefficient.</p> <table><tr><td>Price in rs</td><td>Demand in kgs</td></tr><tr><td>3.80</td><td>3.6</td></tr><tr><td>2.20</td><td>6.0</td></tr><tr><td>2.40</td><td>5.8</td></tr><tr><td>2.60</td><td>5.8</td></tr><tr><td>2.80</td><td>5.0</td></tr><tr><td>3.20</td><td>4.8</td></tr><tr><td>3.00</td><td>4.8</td></tr><tr><td>3.60</td><td>4.2</td></tr><tr><td>3.40</td><td>4.8</td></tr><tr><td>4.00</td><td>3.2</td></tr></table> | Price in rs | Demand in kgs | 3.80 | 3.6 | 2.20 | 6.0 | 2.40 | 5.8 | 2.60 | 5.8 | 2.80 | 5.0 | 3.20 | 4.8 | 3.00 | 4.8 | 3.60 | 4.2 | 3.40 | 4.8 | 4.00 | 3.2 | 10 | 1,2 | 4 | 2.3.2 |
| Price in rs | Demand in kgs | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3.80 | 3.6 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2.20 | 6.0 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2.40 | 5.8 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2.60 | 5.8 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2.80 | 5.0 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3.20 | 4.8 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3.00 | 4.8 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3.60 | 4.2 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3.40 | 4.8 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4.00 | 3.2 | | | | | | | | | | | | | | | | | | | | | | | | | | |

Table 1: Area Under Normal Curve

An entry in the table is the proportion under the entire curve which is between $z = 0$ and a positive value of z . Areas for negative values for z are obtained by symmetry.



Areas of a standard normal distribution

| z | .0 | 0.01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| .0 | .0000 | .0040 | .0080 | .0120 | .0160 | .0199 | .0239 | .0279 | .0319 | .0359 |
| .1 | .0398 | .0438 | .0478 | .0517 | .0557 | .0596 | .0636 | .0675 | .0714 | .0753 |
| .2 | .0793 | .0832 | .0871 | .0910 | .0948 | .0987 | .1026 | .1064 | .1103 | .1141 |
| .3 | .1179 | .1217 | .1255 | .1293 | .1331 | .1368 | .1406 | .1443 | .1480 | .1517 |
| .4 | .1554 | .1591 | .1628 | .1664 | .1700 | .1736 | .1772 | .1808 | .1844 | .1879 |
| .5 | .1915 | .1950 | .1985 | .2019 | .2054 | .2088 | .2123 | .2157 | .2190 | .2224 |
| .6 | .2257 | .2291 | .2324 | .2357 | .2389 | .2422 | .2454 | .2486 | .2517 | .2549 |
| .7 | .2580 | .2611 | .2642 | .2673 | .2703 | .2734 | .2764 | .2794 | .2823 | .2852 |
| .8 | .2881 | .2910 | .2939 | .2967 | .2995 | .3023 | .3051 | .3078 | .3106 | .3133 |
| .9 | .3159 | .3186 | .3212 | .3238 | .3264 | .3289 | .3315 | .3340 | .3365 | .3389 |
| 1.0 | .3413 | .3438 | .3461 | .3485 | .3508 | .3531 | .3554 | .3577 | .3599 | .3621 |
| 1.1 | .3643 | .3665 | .3686 | .3708 | .3729 | .3749 | .3770 | .3790 | .3810 | .3830 |
| 1.2 | .3849 | .3869 | .3888 | .3907 | .3925 | .3944 | .3962 | .3980 | .3997 | .4015 |
| 1.3 | .4032 | .4049 | .4066 | .4082 | .4099 | .4115 | .4131 | .4147 | .4162 | .4177 |
| 1.4 | .4192 | .4207 | .4222 | .4236 | .4251 | .4265 | .4279 | .4292 | .4306 | .4319 |
| 1.5 | .4332 | .4345 | .4357 | .4370 | .4382 | .4394 | .4406 | .4418 | .4429 | .4441 |
| 1.6 | .4452 | .4463 | .4474 | .4484 | .4495 | .4505 | .4515 | .4525 | .4535 | .4545 |
| 1.7 | .4554 | .4564 | .4573 | .4582 | .4591 | .4599 | .4608 | .4616 | .4625 | .4633 |
| 1.8 | .4641 | .4649 | .4656 | .4664 | .4671 | .4678 | .4686 | .4693 | .4699 | .4706 |
| 1.9 | .4713 | .4719 | .4726 | .4732 | .4738 | .4744 | .4750 | .4756 | .4761 | .4767 |
| 2.0 | .4772 | .4778 | .4783 | .4788 | .4793 | .4798 | .4803 | .4808 | .4812 | .4817 |
| 2.1 | .4821 | .4826 | .4830 | .4834 | .4838 | .4842 | .4846 | .4850 | .4854 | .4857 |
| 2.2 | .4861 | .4864 | .4868 | .4871 | .4875 | .4878 | .4881 | .4884 | .4887 | .4890 |
| 2.3 | .4893 | .4896 | .4898 | .4901 | .4904 | .4906 | .4909 | .4911 | .4913 | .4916 |
| 2.4 | .4918 | .4920 | .4922 | .4925 | .4927 | .4929 | .4931 | .4932 | .4934 | .4936 |
| 2.5 | .4938 | .4940 | .4941 | .4943 | .4945 | .4946 | .4948 | .4949 | .4951 | .4952 |
| 2.6 | .4953 | .4955 | .4956 | .4957 | .4959 | .4960 | .4961 | .4962 | .4963 | .4964 |
| 2.7 | .4965 | .4966 | .4967 | .4968 | .4969 | .4970 | .4971 | .4972 | .4973 | .4974 |
| 2.8 | .4974 | .4975 | .4976 | .4977 | .4977 | .4978 | .4979 | .4979 | .4980 | .4981 |
| 2.9 | .4981 | .4982 | .4982 | .4983 | .4984 | .4984 | .4985 | .4985 | .4986 | .4986 |
| 3.0 | .4987 | .4987 | .4987 | .4988 | .4988 | .4989 | .4989 | .4989 | .4990 | .4990 |

Table 2: Critical Values of Student's *t*-Distribution

| d.f. | Level of significance for two-tailed test | | | | | d.f. |
|----------|---|-------|--------|--------|--------|----------|
| | 0.20 | 0.10 | 0.05 | 0.02 | 0.01 | |
| | Level of significance for one-tailed test | | | | | |
| | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 | |
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 | 1 |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 2 |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 3 |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 4 |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 5 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 6 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 7 |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 8 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 9 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 10 |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 11 |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 12 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 13 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 14 |
| 15 | 1.341 | 1.753 | 2.731 | 2.602 | 2.947 | 15 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 16 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 17 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 18 |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 19 |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 20 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 21 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 22 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 23 |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 24 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 25 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 26 |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 27 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 28 |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 29 |
| Infinity | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 | Infinity |

Table 3: Critical Values of χ^2

| Degrees of freedom | Probability under H_0 that of $\chi^2 >$ Chi square | | | | | | |
|--------------------|---|--------|--------|--------|--------|--------|--------|
| | .99 | .95 | .50 | .10 | .05 | .02 | .01 |
| 1 | .000157 | .00393 | .455 | 2.706 | 3.841 | 5.412 | 6.635 |
| 2 | .0201 | .103 | 1.386 | 4.605 | 5.991 | 7.824 | 9.210 |
| 3 | .115 | .352 | 2.366 | 6.251 | 7.815 | 9.837 | 11.341 |
| 4 | .297 | .711 | 3.357 | 7.779 | 9.488 | 11.668 | 13.277 |
| 5 | .554 | 1.145 | 4.351 | 9.236 | 11.070 | 13.388 | 15.086 |
| 6 | .872 | 1.635 | 5.348 | 10.645 | 12.592 | 15.033 | 16.812 |
| 7 | 1.239 | 2.167 | 6.346 | 12.017 | 14.067 | 16.622 | 18.475 |
| 8 | 1.646 | 2.733 | 7.344 | 13.362 | 15.507 | 18.168 | 20.090 |
| 9 | 2.088 | 3.325 | 8.343 | 14.684 | 16.919 | 19.679 | 21.666 |
| 10 | 2.558 | 3.940 | 9.342 | 15.987 | 18.307 | 21.161 | 23.209 |
| 11 | 3.053 | 4.575 | 10.341 | 17.275 | 19.675 | 22.618 | 24.725 |
| 12 | 3.571 | 5.226 | 11.340 | 18.549 | 21.026 | 24.054 | 26.217 |
| 13 | 4.107 | 5.892 | 12.340 | 19.812 | 22.362 | 25.472 | 27.688 |
| 14 | 4.660 | 6.571 | 13.339 | 21.064 | 23.685 | 26.873 | 29.141 |
| 15 | 4.229 | 7.261 | 14.339 | 22.307 | 24.996 | 28.259 | 30.578 |
| 16 | 5.812 | 7.962 | 15.338 | 23.542 | 26.296 | 29.633 | 32.000 |
| 17 | 6.408 | 8.672 | 16.338 | 24.769 | 27.587 | 30.995 | 33.409 |
| 18 | 7.015 | 9.390 | 17.338 | 25.989 | 28.869 | 32.346 | 34.805 |
| 19 | 7.633 | 10.117 | 18.338 | 27.204 | 30.144 | 33.687 | 36.191 |
| 20 | 8.260 | 10.851 | 19.337 | 28.412 | 31.410 | 35.020 | 37.566 |
| 21 | 8.897 | 11.591 | 20.337 | 29.615 | 32.671 | 36.343 | 38.932 |
| 22 | 9.542 | 12.338 | 21.337 | 30.813 | 33.924 | 37.659 | 40.289 |
| 23 | 10.196 | 13.091 | 22.337 | 32.007 | 35.172 | 38.968 | 41.638 |
| 24 | 10.856 | 13.848 | 23.337 | 32.196 | 36.415 | 40.270 | 42.980 |
| 25 | 11.524 | 14.611 | 24.337 | 34.382 | 37.652 | 41.566 | 44.314 |
| 26 | 12.198 | 15.379 | 25.336 | 35.363 | 38.885 | 41.856 | 45.642 |
| 27 | 12.879 | 16.151 | 26.336 | 36.741 | 40.113 | 44.140 | 46.963 |
| 28 | 13.565 | 16.928 | 27.336 | 37.916 | 41.337 | 45.419 | 48.278 |
| 29 | 14.256 | 17.708 | 28.336 | 39.087 | 42.557 | 46.693 | 49.588 |
| 30 | 14.953 | 18.493 | 29.336 | 40.256 | 43.773 | 47.962 | 50.892 |

Note: For degrees of freedom greater than 30, the quantity $2\chi^2 - \sqrt{2d.f. - 1}$ may be used as a normal variate with unit variance i.e., $z_\alpha = \sqrt{2\chi^2} - \sqrt{2d.f. - 1}$.

Table 4(a): Critical Values of F-Distribution (at 5 per cent)

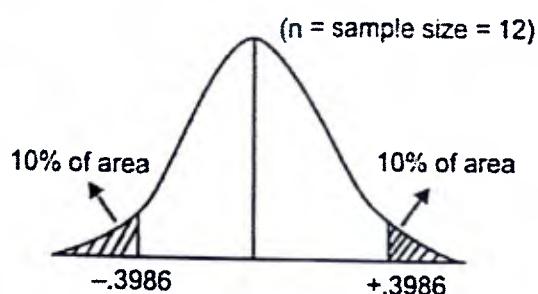
| $v_1 \backslash v_2$ | 1 | 2 | 3 | 4 | 5 | 6 | 8 | 12 | 24 | ∞ |
|----------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1 | 161.4 | 199.5 | 215.7 | 224.6 | 230.2 | 234.0 | 238.9 | 243.9 | 249.1 | 243.3 |
| 2 | 18.51 | 19.00 | 19.16 | 19.25 | 19.30 | 19.33 | 19.37 | 19.41 | 19.45 | 19.50 |
| 3 | 10.13 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.85 | 8.74 | 8.64 | 8.53 |
| 4 | 7.71 | 6.94 | 6.59 | 6.39 | 6.26 | 6.16 | 6.04 | 5.91 | 5.77 | 5.63 |
| 5 | 6.61 | 5.79 | 5.41 | 5.19 | 5.05 | 4.95 | 4.82 | 4.68 | 4.53 | 4.36 |
| 6 | 5.99 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.15 | 4.00 | 3.84 | 3.67 |
| 7 | 5.59 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.73 | 3.57 | 3.41 | 3.23 |
| 8 | 5.32 | 4.46 | 4.07 | 3.84 | 3.69 | 3.58 | 3.44 | 3.28 | 3.12 | 2.93 |
| 9 | 5.12 | 4.26 | 3.86 | 3.63 | 3.48 | 3.37 | 3.23 | 3.07 | 2.90 | 2.71 |
| 10 | 4.96 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.07 | 2.91 | 2.74 | 2.54 |
| 11 | 4.84 | 3.98 | 3.59 | 3.36 | 3.20 | 3.09 | 2.95 | 2.79 | 2.61 | 2.40 |
| 12 | 4.75 | 3.88 | 3.49 | 3.26 | 3.11 | 3.00 | 2.85 | 2.69 | 2.51 | 2.30 |
| 13 | 4.67 | 3.80 | 3.41 | 3.18 | 3.02 | 2.92 | 2.77 | 2.60 | 2.42 | 2.21 |
| 14 | 4.60 | 3.74 | 3.34 | 3.11 | 2.96 | 2.85 | 2.70 | 2.53 | 2.35 | 2.13 |
| 15 | 4.54 | 3.68 | 3.29 | 3.06 | 2.90 | 2.79 | 2.64 | 2.48 | 2.29 | 2.07 |
| 16 | 4.49 | 3.63 | 3.24 | 3.01 | 2.85 | 2.74 | 2.59 | 2.42 | 2.24 | 2.01 |
| 17 | 4.45 | 3.59 | 3.20 | 2.96 | 2.81 | 2.70 | 2.55 | 2.38 | 2.19 | 1.96 |
| 18 | 4.41 | 3.55 | 3.16 | 2.93 | 2.77 | 2.66 | 2.51 | 2.34 | 2.15 | 1.92 |
| 19 | 4.38 | 3.52 | 3.13 | 2.90 | 2.74 | 2.63 | 2.48 | 2.31 | 2.11 | 1.88 |
| 20 | 4.35 | 3.49 | 3.10 | 2.87 | 2.71 | 2.60 | 2.45 | 2.28 | 2.08 | 1.84 |
| 21 | 4.32 | 3.47 | 3.07 | 2.84 | 2.68 | 2.57 | 2.42 | 2.25 | 2.05 | 1.81 |
| 22 | 4.30 | 3.44 | 3.05 | 2.82 | 2.66 | 2.55 | 2.40 | 2.23 | 2.03 | 1.78 |
| 23 | 4.28 | 3.42 | 3.03 | 2.80 | 2.64 | 2.53 | 2.38 | 2.20 | 2.01 | 1.76 |
| 24 | 4.26 | 3.40 | 3.01 | 2.78 | 2.62 | 2.51 | 2.36 | 2.18 | 1.98 | 1.73 |
| 25 | 4.24 | 3.38 | 2.99 | 2.76 | 2.60 | 2.49 | 2.34 | 2.16 | 1.96 | 1.71 |
| 26 | 4.22 | 3.37 | 2.98 | 2.74 | 2.59 | 2.47 | 2.32 | 2.15 | 1.95 | 1.69 |
| 27 | 4.21 | 3.35 | 2.96 | 2.73 | 2.57 | 2.46 | 2.31 | 2.13 | 1.93 | 1.67 |
| 28 | 4.20 | 3.34 | 2.95 | 2.71 | 2.56 | 2.45 | 2.29 | 2.12 | 1.91 | 1.65 |
| 29 | 4.18 | 3.33 | 2.93 | 2.70 | 2.54 | 2.43 | 2.28 | 2.10 | 1.90 | 1.64 |
| 30 | 4.17 | 3.32 | 2.92 | 2.69 | 2.53 | 2.42 | 2.27 | 2.09 | 1.89 | 1.62 |
| 40 | 4.08 | 3.23 | 2.84 | 2.61 | 2.45 | 2.34 | 2.18 | 2.00 | 1.79 | 1.51 |
| 60 | 4.00 | 3.15 | 2.76 | 2.52 | 2.37 | 2.25 | 2.10 | 1.92 | 1.70 | 1.39 |
| 120 | 3.92 | 3.07 | 2.68 | 2.45 | 2.29 | 2.17 | 2.02 | 1.83 | 1.61 | 1.25 |
| ∞ | 3.84 | 2.99 | 2.60 | 2.37 | 2.21 | 2.10 | 1.94 | 1.75 | 1.52 | 1.00 |

 v_1 = Degrees of freedom for greater variance. v_2 = Degrees of freedom for smaller variance.

Table 4(b): Critical Values of *F*-Distribution (at 1 per cent)

| $\begin{matrix} v_1 \\ v_2 \end{matrix}$ | 1 | 2 | 3 | 4 | 5 | 6 | 8 | 12 | 24 | ∞ |
|--|-------|--------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1 | 4052 | 4999.5 | 5403 | 5625 | 5764 | 5859 | 5982 | 6106 | 6235 | 6366 |
| 2 | 98.50 | 99.00 | 99.17 | 99.25 | 99.30 | 99.33 | 99.37 | 99.42 | 99.46 | 99.50 |
| 3 | 34.12 | 30.82 | 29.46 | 28.71 | 28.24 | 27.91 | 27.49 | 27.05 | 26.60 | 26.13 |
| 4 | 21.20 | 18.00 | 16.69 | 15.98 | 15.52 | 15.21 | 14.80 | 14.37 | 13.93 | 13.45 |
| 5 | 16.26 | 13.27 | 12.06 | 11.39 | 10.97 | 10.67 | 10.29 | 9.89 | 9.47 | 9.02 |
| 6 | 13.75 | 10.92 | 9.78 | 9.15 | 8.75 | 8.47 | 8.10 | 7.72 | 7.31 | 6.88 |
| 7 | 12.25 | 9.55 | 8.45 | 7.85 | 7.46 | 7.19 | 6.84 | 6.47 | 6.07 | 5.65 |
| 8 | 11.26 | 8.65 | 7.59 | 7.01 | 6.63 | 6.37 | 6.03 | 5.67 | 5.28 | 4.86 |
| 9 | 10.56 | 8.02 | 6.99 | 6.42 | 6.06 | 5.80 | 5.47 | 5.11 | 4.73 | 4.31 |
| 10 | 10.04 | 7.56 | 6.55 | 5.99 | 5.64 | 5.39 | 5.06 | 4.71 | 4.33 | 3.91 |
| 11 | 9.65 | 7.21 | 6.22 | 5.87 | 5.52 | 5.27 | 4.94 | 4.59 | 4.21 | 3.79 |
| 12 | 9.33 | 6.93 | 5.95 | 5.61 | 5.26 | 5.01 | 4.68 | 4.33 | 3.95 | 3.53 |
| 13 | 9.07 | 6.70 | 5.74 | 5.41 | 5.06 | 4.81 | 4.48 | 4.13 | 3.75 | 3.33 |
| 14 | 8.86 | 6.51 | 5.56 | 5.24 | 4.89 | 4.64 | 4.31 | 3.96 | 3.58 | 3.16 |
| 15 | 8.68 | 6.36 | 5.42 | 5.10 | 4.75 | 4.50 | 4.17 | 3.82 | 3.44 | 3.02 |
| 16 | 8.53 | 6.23 | 5.29 | 4.97 | 4.62 | 4.37 | 4.04 | 3.69 | 3.31 | 2.89 |
| 17 | 8.40 | 6.11 | 5.18 | 4.86 | 4.51 | 4.26 | 3.93 | 3.58 | 3.20 | 2.78 |
| 18 | 8.29 | 6.01 | 5.09 | 4.77 | 4.42 | 4.17 | 3.84 | 3.49 | 3.11 | 2.69 |
| 19 | 8.18 | 5.93 | 5.01 | 4.69 | 4.34 | 4.09 | 3.76 | 3.41 | 3.03 | 2.61 |
| 20 | 8.10 | 5.85 | 4.94 | 4.62 | 4.27 | 4.02 | 3.69 | 3.34 | 2.96 | 2.54 |
| 21 | 8.02 | 5.78 | 4.87 | 4.55 | 4.20 | 3.95 | 3.62 | 3.27 | 2.89 | 2.47 |
| 22 | 7.95 | 5.72 | 4.82 | 4.50 | 4.15 | 3.90 | 3.57 | 3.22 | 2.84 | 2.42 |
| 23 | 7.88 | 5.66 | 4.76 | 4.44 | 4.09 | 3.84 | 3.51 | 3.16 | 2.78 | 2.36 |
| 24 | 7.82 | 5.61 | 4.72 | 4.40 | 4.05 | 3.80 | 3.47 | 3.12 | 2.74 | 2.32 |
| 25 | 7.77 | 5.57 | 4.68 | 4.36 | 4.01 | 3.76 | 3.43 | 3.08 | 2.70 | 2.28 |
| 26 | 7.72 | 5.53 | 4.64 | 4.32 | 3.97 | 3.72 | 3.39 | 3.04 | 2.66 | 2.24 |
| 27 | 7.68 | 5.49 | 4.60 | 4.28 | 3.93 | 3.68 | 3.35 | 3.00 | 2.62 | 2.20 |
| 28 | 7.64 | 5.45 | 4.57 | 4.25 | 3.90 | 3.65 | 3.32 | 2.97 | 2.59 | 2.17 |
| 29 | 7.60 | 5.42 | 4.54 | 4.22 | 3.87 | 3.62 | 3.29 | 2.94 | 2.56 | 2.14 |
| 30 | 7.56 | 5.39 | 4.51 | 4.19 | 3.84 | 3.59 | 3.26 | 2.91 | 2.53 | 2.11 |
| 40 | 7.31 | 5.18 | 4.31 | 4.00 | 3.65 | 3.40 | 3.07 | 2.72 | 2.34 | 1.92 |
| 60 | 7.08 | 4.98 | 4.13 | 3.83 | 3.48 | 3.23 | 2.90 | 2.55 | 2.17 | 1.75 |
| 120 | 6.85 | 4.79 | 3.95 | 3.65 | 3.30 | 3.05 | 2.72 | 2.37 | 1.99 | 1.57 |
| ∞ | 6.64 | 4.60 | 3.78 | 3.32 | 3.02 | 2.80 | 2.51 | 2.18 | 1.79 | 1.00 |

 v_1 = Degrees of freedom for greater variance. v_2 = Degrees of freedom for smaller variance.

Table 5: Values for Spearman's Rank Correlation (r) for Combined Areas in Both Tails

| n | .20 | .10 | .05 | .02 | .01 | .002 |
|-----|-------|-------|-------|-------|-------|-------|
| 4 | .8000 | .8000 | — | — | — | — |
| 5 | .7000 | .8000 | .9000 | .9000 | — | — |
| 6 | .6000 | .7714 | .8236 | .8857 | .9429 | — |
| 7 | .5357 | .6786 | .7450 | .8571 | .8929 | .9643 |
| 8 | .5000 | .6190 | .7143 | .8095 | .8571 | .9286 |
| 9 | .4667 | .5833 | .6833 | .7667 | .8167 | .9000 |
| 10 | .4424 | .5515 | .6364 | .7333 | .7818 | .8667 |
| 11 | .4182 | .5273 | .6091 | .7000 | .7455 | .8364 |
| 12 | .3986 | .4965 | .5804 | .6713 | .7273 | .8182 |
| 13 | .3791 | .4780 | .5549 | .6429 | .6978 | .7912 |
| 14 | .3626 | .4593 | .5341 | .6220 | .6747 | .7670 |
| 15 | .3500 | .4429 | .5179 | .6000 | .6536 | .7464 |
| 16 | .3382 | .4265 | .5000 | .5824 | .6324 | .7265 |
| 17 | .3260 | .4118 | .4853 | .5637 | .6152 | .7083 |
| 18 | .3148 | .3994 | .4716 | .5480 | .5975 | .6904 |
| 19 | .3070 | .3895 | .4579 | .5333 | .5825 | .6737 |
| 20 | .2977 | .3789 | .4451 | .5203 | .5684 | .6586 |
| 21 | .2909 | .3688 | .4351 | .5078 | .5545 | .6455 |
| 22 | .2829 | .3597 | .4241 | .4963 | .5426 | .6318 |
| 23 | .2767 | .3518 | .4150 | .4852 | .5306 | .6186 |
| 24 | .2704 | .3435 | .4061 | .4748 | .5200 | .6070 |
| 25 | .2646 | .3362 | .3977 | .4654 | .5100 | .5962 |
| 26 | .2588 | .3299 | .3894 | .4564 | .5002 | .5856 |
| 27 | .2540 | .3236 | .3822 | .4481 | .4915 | .5757 |
| 28 | .2480 | .3175 | .3749 | .4401 | .4828 | .5660 |
| 29 | .2443 | .3113 | .3685 | .4320 | .4744 | .5567 |
| 30 | .2400 | .3059 | .3620 | .4251 | .4665 | .5479 |



Bharatiya Vidya Bhavan's



Sardar Patel College of Engineering
(A Government Aided Autonomous Institute)
Munshi Nagar, Andheri (West), Mumbai – 400058.

End Semester Examination

M.Tech (Civil Engg) in Constr. mgmt. Sem I

Date: 22/4/2022

Total points: 100

Duration: 10:00am-1:00pm

Class: M.TECH (CM).

Semester: I

Program: Civil

Name of the Course: Management of Housing Projects

Code: MTCMPEC 123

Instructions:

Attempt any 5 questions:-

| Q. No | | Points | CO | BL | PI |
|-------|--|------------------|------------------|------------------|----------------------------------|
| 1. | Discuss in detail:- a. Illustrate the difference in Rural and Urban housing. Explain in detail PMAY. b. Explain the concept of Affordable housing. Also discuss "Housing for All" with reference to government of Maharashtra. | 10 10 | 2 2 | 4 3 | 7.1.2 7.1.2 |
| 2. | Write Short Notes on:- a. Innovative materials & construction techniques b. Low cost housing c. Mass housing d. Industrialized housing | 5 5 5 5 | 1 1 1 1 | 3 2 2 2 | 5.4.1 5.4.1 5.4.1 5.4.1 |
| 3. | a. What are the main reasons for project failure? b. What are Roles and Responsibilities a project manager should have? | 10 10 | 1 1 | 4 4 | 5.4.1 5.4.1 |
| 4. | a. Discuss in detail Heat Ventilation & Air-Conditioning System with reference to functions and types of HVAC systems. b. Plumbing system | 10 10 | 1 1 | 5 5 | 6.3.1 6.3.1 |

| | | | | | |
|----|---|----|---|---|-------|
| 5. | a. Why maintenance is important in building? | 10 | 2 | 4 | 6.3.1 |
| | b. What is maintenance and repair of building? | 10 | 2 | 4 | 6.3.1 |
| 6. | a. Discuss Estate Management with respect to MHADA-Maharashtra Housing and Area Development Board. | 10 | 1 | 3 | |
| | b. Short Note on Estate Management | 10 | 1 | 3 | |
| 7. | a. What are the objects and reasons for which the Real Estate (Regulation and Development) Act 2016 has been framed? | 10 | 2 | 4 | 7.1.2 |
| | | 5 | 2 | 4 | 7.1.2 |
| | b. Is it mandatory for the promoter to obtain permissions for the real estate project before applying for registration to MahaRERA? | 5 | 2 | 4 | 7.1.2 |
| | c. In case of delay in getting possession from the promoter, will the buyer be entitled to get interest on the amount paid by him, for such delayed period? | | | | |



Bharatiya Vidya Bhavan's



Sardar Patel College of Engineering
(A Government Aided Autonomous Institute)
Munshi Nagar, Andheri (West), Mumbai – 400058.

Re-Exam Semester Examination

E.Y. M. Tech (Construction) Sem I

Total points: 100

Date: 21/7/2022

Duration: 2:00pm-5:00pm

Class: M.TECH (CM).

Semester: I

Program: Civil

Name of the Course: Management of Housing Projects

Code: MTCMPEC 123

Instructions:

Attempt any 5 questions:-

| Q. No | | Points | CO | BL | PI |
|-------|---|----------|--------|--------|----------------|
| 1. | Discuss in detail:- a. Explain the contribution of various national and state level agencies in housing development. b. Illustrate the national housing policy. | 10 10 | 2 2 | 4 3 | 7.1.2 7.1.2 |
| 2. | Write Short Notes on:- a. Innovative materials b. Low cost housing | 10 10 | 1 1 | 3 2 | 5.4.1 5.4.1 |
| 3. | a. Describe causes for project failure? b. What are Roles and Responsibilities a project manager should have? | 10 10 | 1 1 | 4 4 | 5.4.1 5.4.1 |
| 4. | a. Importance of Building services in any building environment. b. HVAC system | 10 10 | 1 1 | 5 5 | 6.3.1 6.3.1 |
| 5. | a. Why maintenance is important in building? b. What is maintenance and repair of building? | 10 10 | 2 2 | 4 4 | 6.3.1 6.3.1 |
| 6. | a. Discuss MHADA in detail. b. Short Note on Estate Management | 10 10 | 1 1 | 3 3 | 7.1.2 7.1.2 |
| 7. | a. Illustrate RERA in detail? b. Explain Slum Rehabilitation policies. | 10 10 | 2 2 | 4 3 | 7.1.2 7.1.2 |



Bharatiya Vidya Bhavan's

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Munshi Nagar, Andheri (West), Mumbai - 400058.

END SEMESTER EXAMINATION



Total points:100

Duration: 3 Hr

Date: 11/4/2022

First year M.Tech - Civil Engg (Construction Mgt) Sem I

Class: M.TECH (CM).

Semester: I

Program: Civil

Name of the Course: Construction Organisation & Safety Management Course

Code : PC-MTCM-101

Instructions:

Attempt any 5 questions

| Q. No. | | Points | CO | BL | PI |
|--------|--|--------|----|----|-------|
| 1 | a. Illustrate the theory of Fredrick Taylor -Scientific management approach, with current scenario of construction industry. | 10 | 1 | 4 | 2.3.1 |
| | b. Discuss in detail Characteristic of Management with the help of following salient features: 1. Economic Resources 2. Goal Oriented 3. Distinct Process 4.Integrative Role 5.System of Authority 6.Multi-disciplinary Subject 7.Universal Application | 10 | 1 | 4 | 2.1.1 |
| 2 | a. What are the qualities of project Manager? | 5 | 2 | 3 | 8.3.1 |
| | b. Explain role of organizational leader in team development and conflict management? | 10 | 3 | 3 | 2.1.1 |
| | c. What is Motivation? Why is it important? What are various ways of motivation in general context? | 5 | 1 | 3 | 2.1.1 |
| 3 | a. Illustrate with the help of flow-chart relationship between time and motion study to work study. | 10 | 1 | 4 | 2.5.3 |
| | b. Write a short note on : Work Measurement | 10 | 1 | 4 | 2.5.3 |
| 4 | a. Roles, responsibilities and duties of site managers, safety officers, general employee and safety committee. | 10 | 2 | 3 | 7.3.2 |
| | b. Importance of safety training, incentives and monitoring in construction safety. | 10 | 2 | 5 | 7.3.2 |
| 5 | a. What are different accidents that can occur on various construction site during different stages of construction? | 10 | 1 | 3 | 6.3.1 |
| | b. Safety during use of construction equipment. | 10 | 3 | 3 | 6.3.1 |
| 6 | a. Write a note on: First Aid on site. | 10 | 1 | 4 | 6.3.1 |
| | b. What are labor laws, legal requirement and cost aspect of accidents on site? | 10 | 2 | 5 | 6.4.1 |
| 7 | a. Equipment and training provided on any ISO approved Construction Company. | 10 | 3 | 4 | 6.4.1 |
| | b. Safety audit and OSHA guidelines. | 10 | 3 | 4 | 6.4.1 |



Bharatiya Vidya Bhavan's
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Munshi Nagar, Andheri (West), Mumbai – 400058.

Examinations, April 2022



First year M.Tech (Civil Engg in) Constn.

Total points: 100

Date-18/4/2022

Duration: 3 Hours

Class: M.TECH(CM).

Semester: I

Program: Civil

Name of the Course:

Accounting and Finance Management

Course Code :

PECMTCM 103

Instructions:

1. Attempt any five
2. Draw neat diagrams
3. Assume suitable data if necessary and state the clearly.

| Que. No | | Points | CO | BL | PI | | | | | | | | | | | | |
|---------|---|-----------------|-----------------|-----------------|-------|-----------|---------|---|--------|-----------|---|--------|--------|---|---|---|-------|
| Q1 (A) | Mr. Sharma will retire after 34 years from now. He expects that he will live 26 years after retirement. He wants to have enough money upon reaching the retirement age to withdraw INR 5,00,000 from the account at the beginning of each year he expects to live after retirement, and yet he wants to have INR 35,00,000 left in account at the time of his expected death (i.e., 60 years from now). He plans to accumulate retirement funds by making equal deposits at the end of each year for the next 34 years from now. He expects that he will be able to earn 14% per annum on his deposits. However, he only expects 7 % interest per annum after retirement (he will choose to place his money in less risky investments). What equal annual instalment should he make each year to reach his retirement goal? | 6 | 1 | 4 | 1.1.1 | | | | | | | | | | | | |
| Q1(B) | <p>Company named XYZ limited is considering two project investment options (i.e., Project A and Project B), both of which initially cost INR 20 lakhs. Further cash-inflows of both the project are given in following table</p> <table><tr><th>Year</th><th>Project A (INR)</th><th>Project B (INR)</th></tr><tr><td>1</td><td>1,000,000</td><td>900,000</td></tr><tr><td>2</td><td>600000</td><td>1,000,000</td></tr><tr><td>3</td><td>800000</td><td>600000</td></tr></table> <p>Based on the payback period method, which of the project should be chosen?</p> <p>A. Project A which has a payback period of 2 years and 8 months</p> <p>B. Project A which has a payback period of 2 years and 6 months</p> <p>C. Project B which has a payback period of 2 years and 2 months</p> <p>D. Project B which has a payback period of 2 years and 6 months</p> <p>Rohit has purchased a new motor bike for INR 120,000. He was able to make a down payment equal to 20% of the value of the motorbike; the balance was loaned</p> | Year | Project A (INR) | Project B (INR) | 1 | 1,000,000 | 900,000 | 2 | 600000 | 1,000,000 | 3 | 800000 | 600000 | 6 | 3 | 3 | 3.3.1 |
| Year | Project A (INR) | Project B (INR) | | | | | | | | | | | | | | | |
| 1 | 1,000,000 | 900,000 | | | | | | | | | | | | | | | |
| 2 | 600000 | 1,000,000 | | | | | | | | | | | | | | | |
| 3 | 800000 | 600000 | | | | | | | | | | | | | | | |
| | | 8 | 2 | 3 | 1.1.2 | | | | | | | | | | | | |

| | | | | | |
|--------|---|----|---|---|-------|
| Q 1(C) | by the bank. The interest rate charged by the bank is 14% compounded quarterly. The loan must be returned in a 5-year period by equal yearly payments. What is the value of the yearly instalments that Rohit must pay? | | | | |
| Q2(A) | <p>The initial cost of a piece of construction equipment is Rs.30,00,000 having a useful life of 10 years. The estimated salvage value of the equipment at the end of the useful life is Rs.450,000.</p> <ol style="list-style-type: none"> 1. The book value of the construction equipment at the end of 5th year using Straight -line method is _____ 2. The book value of the construction equipment at the end of 5th year (BV5) and depreciation (d5) for 5th year using Double-declining balance method are _____ 3. Determine the book value (BV5) of the construction equipment at the end of 5th year and depreciation (d5) for 5th year using Sum-of-the-years-digits method _____ 4. Determine accumulated depreciation at the end of 5th year using Sinking fund method, if interest rate is 8.2 % per year _____ | 16 | 2 | 4 | 1.1.2 |
| Q2(B) | <p>A consultant proposes two designs (Type 'A' and Type 'B') for a bridge to be constructed across a river. Type 'A' design of a bridge costs INR 45 crores and an expense of INR 3 crores every year to operate and maintain it. Type 'B' design of bridge costs INR 60 crores and an expense of INR 1.5 crores every year to operate and maintain it. Both the designs have considered 100 years as the design life of the bridge. The minimum required rate of return is 8 percent.</p> <p>Which of the following options is the best recommendation based on the information provided above?</p> <p>A. Go-ahead with Type 'A' design as it has lower initial investment B. Go- ahead with Type 'B' design as it has lower operating and maintenance cost C. Go-ahead with Type 'A' design as its net present worth is INR 825,000,000 D. Go-ahead with Type 'B' design as its net present worth is INR 787,000,000</p> | 4 | 3 | 3 | 1.2.2 |
| Q3(A) | A piece of land was purchased at INR 40 lakhs. An investment of an additional INR 20 lakhs was made to construct a small shopping complex on this land. The complex is expected to fetch an annual rental of INR 75,000 to the owner, while the cost towards its upkeep, tax, etc., is expected to be INR 30,000 annually. The owner plans to sell the entire plot with constructed facilities at an expected price of INR 120 lakhs at the end of five years. What percent rate of return will be earned by the owner on this investment? | 4 | 1 | 4 | 1.2.3 |
| Q3(B) | Consider the following information with respect to two projects (Project 'A' and Project 'B') provided in the table. | 10 | 2 | 4 | 1.1.2 |

| End of year Cash flows (INR) | 0 | 1 | 2 | 3 |
|------------------------------------|---------|-------|-------|-------|
| Project 'A' | -50,000 | 9,000 | 18500 | 45000 |
| Project 'B' | -50,000 | 45000 | 15000 | 17000 |

Assume minimum attractive rate of return to is 10 percent.

1. Using computations based on present worth method, which of the following sets correctly represents the net present worth of both the projects?

A. Net Present Worth Project 'A' is INR 22,500 and Net Present Worth of Project 'B' is INR 27000

B. Net Present Worth Project 'A' is INR 27,000 and Net Present Worth of Project 'B' is INR 22,500 C. Net Present Worth Project 'A' is INR 7,280 and Net Present Worth of Project 'B' is INR 16,078

D. Net Present Worth Project 'A' is INR 16,078 and Net Present Worth of Project 'B' is INR 7,280

2. Using computations based on annual worth method, choose the best alternative.

A. Chose Project 'A' as its Annual Worth is INR 2,927

B. Chose Project 'A' as its Annual Worth is INR 7,280 C. Chose Project 'B' as its Annual Worth is INR 6,465

D. Chose Project 'B' as its Annual Worth is INR 16,078

3. What is Net Present Worth based on difference in cashflows of two projects (i.e., Project 'A' - Project 'B').

6

4

3

1.1.3

Q3(C)

Two pumps can be used for pumping a corrosive liquid. A pump with a brass impeller costs INR 40,000 and is expected to last for three years. A pump with a stainless-steel impeller will cost INR 95,000 and lasts for five years. An overhaul costing INR 15,000 will be required after 2000 operating hours of brass one while an overhaul of INR 35,000 for stainless steel after 9000 hours. If the operating cost of each pump is INR 25/hour, how many hours /year (rounded off to nearest integer) must the pump be required to justify the purchase of an expensive pump? Interest rate 10% per year

Q4(A)

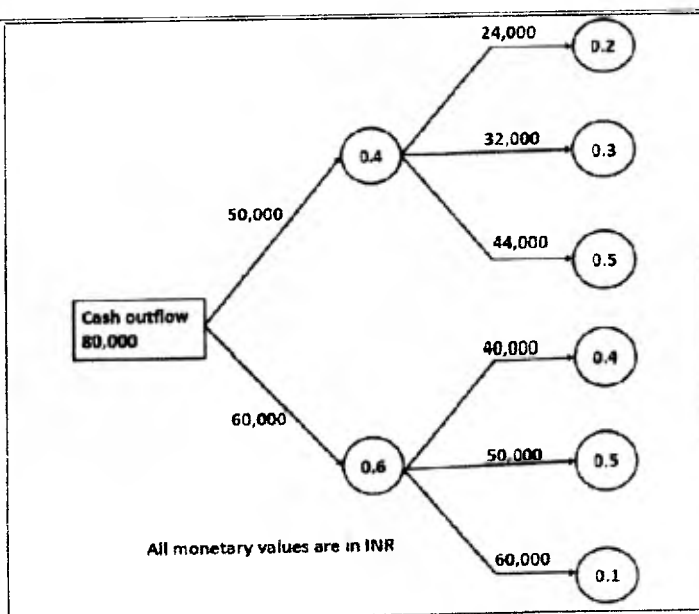
The estimates of the cash inflows after taxes (CFAT) for a proposed project, whose expected life is 2 years, are shown in the given decision tree. As shown, the initial investment needed for the project is INR 80,000. The cash inflows are shown on arrows and the associated probabilities are shown inside the circles. Assuming that there is no correlation between the cash inflows of two years, and, that the annual interest rate is 10%, what is the expected net present value (in INR) of the proposed project.

10

1

5

1.3.1



Q4(B)

An equipment (called the defender equipment) that was purchased at a cost of INR 23,000 four years ago is considered for replacement against a challenger whose cost is INR 25,000. The existing equipment can be traded in today at INR 6,500, and if kept for another 6 years, it will have a salvage value of INR 2,200. The annual maintenance cost of the existing asset is INR 7,500 and that of the challenger is INR 3,700. The challenger equipment has a salvage value is INR 3, 200 at the end of year 10. Assuming the rate of interest to be 15%, answer the following questions

1. What is the equivalent annual cost (in INR) of the defender equipment?
2. What is the equivalent annual cost (in INR) of the challenger equipment?
3. What is the sunk cost (in INR)?

10

3

3

1.3.2

Q5(A)

For a given project, the contractor has estimated the direct cost and indirect cost of labor, material, and plant (given in the Table). The contractor plans to apply an off top of 15%, 10% and 10% on labor, material, and plant respectively.

| Description | Labor | Material | Plant |
|--------------------|-------|----------|-------|
| Direct cost (\$) | 100 | 700 | 50 |
| Indirect cost (\$) | 80 | 35 | 5 |
| Off top (%) | 15 | 10 | 10 |

1. Which of the following options give the correct combination of the bid price (without tax consideration) to be applied on labor, material, and plant?

- A. Labor: \$112; Material: \$717; Plant: \$51
- B. Labor: \$212; Material: \$817; Plant: \$61
- C. Labor: \$112; Material: \$817; Plant: \$61
- D. Labor: \$212; Material: \$717; Plant: \$51

2. Which of the following options give the correct combination of the cover (multiplication factor) that needs to be applied on labor, material, and subcontractor costs?

- A. Labor: 2.64; Material: 15.33; Plant: 12.22
- B. Labor: 2.12; Material: 2.17; Plant: 1.22

7

2

2

1.3.1

C. Labor: 2.12; Material: 1.17; Plant: 1.22
D. Labor: 2.64; Material: 23.33; Plant: 12.22

Q5(B)

Transit Mixers (used to transport concrete to placing locations) arrive at a batching plant from different sites in an area served by a common ready mix concrete plant. The arrival time intervals of the Transit Mixers are observed and yield the following results.

| Arrival time interval (minutes) | Frequency |
|---------------------------------|-----------|
| 2 | 10 |
| 3 | 15 |
| 4 | 30 |
| 5 | 25 |
| 6 | 20 |

The time taken to load the Transit Mixers which are either 6 or 9 cum capacity are constant at 3 and 5 minutes respectively, and both types are equally represented (equal probability) at the depot.

Start the trial from 10:00 AM and assume no Transit Mixer is waiting currently. Random numbers to be used for the computations are given with the question.

If the batching plant loads each of the Transit Mixer immediately it arrives, calculate the following corresponding to the first six trials only:

1. What is the total time (in minutes) likely that the Batching Plant will be waiting?
2. What is the total time (in minutes) likely that the Transit Mixers will be waiting?

Two Digit Random Number Table-

52 06 50 8853 30 10 47 99 37 66 91 35 32 00 84 57 07
37 63 28 02 74 35 24 03 29 60 74 85 90 73 59 55 17 60
82 57 68 28 05 94 03 11 27 79 90 87 92 41 09 25 36 77
69 02 36 49 71 99 32 10 75 21 95 90 94 38 97 71 72 49
98 94 90 36 06 78 23 67 89 85 29 21 25 73 69 34 85 76
96 52 62 87 49 56 59 23 78 71 72 90 57 01 98 57 31 95
33 69 27 21 11 60 95 89 68 48 17 89 34 09 93 50 44 51
50 33 50 95 13 44 34 62 64 39 55 29 30 64 49 44 30 16
88 32 18 50 62 57 34 56 62 31 15 40 90 34 51 95 26 14
90 30 36 24 69 82 51 74 30 35 36 85 01 55 92 64 09 85
50 48 61 18 85 23 08 54 17 12 80 69 24 84 92 16 49 59
27 88 21 62 69 64 48 31 12 73 02 68 00 16 16 46 13 85
45 14 46 32 13 49 66 62 74 41 86 98 92 98 84 54 33 40
81 02 01 78 82 74 97 37 45 31 94 99 42 49 27 64 89 42
66 83 14 74 27 76 03 33 11 97 59 81 72 00 64 61 13 52
74 05 82 82 93 09 96 33 52 78 13 06 28 30 94 23 37 39
30 34 87 01 74 11 46 82 59 94 25 34 32 23 17 01 58 73

6

3

4

1.2.3

7

4

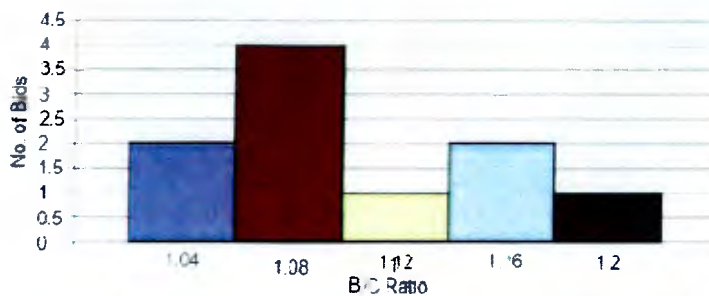
3

1.2.3

Q5(C)

Analysis of the bidding behavior of a typical competitor (Y) against you, reveals that the ratio of his bid (B) to your cost (C) in 10 previous bids take the following histogram. For the computation of standard deviation use the following formula.

$$\sigma = \sqrt{\frac{\sum [(x - \mu)^2 \times f(x)]}{n - 1}}$$



1. Based on that behavior, what is the mark-up value that this competitor uses on average?
2. What is the probability of your winning against this competitor if you use a markup of 14%?
3. In a new project with a cost of INR1,000,000 estimated cost, what is your optimum markup strategy (in terms of markup percentage) against four typical competitors using Friedman's model?

Q6(A) Explain Break-even analysis.

4

4

2

2.1.3

Q6(B) Calculate payback period of following projects each requiring a cash outlay of Rs. 12000. Suggest which one acceptable id standard payback period is 6 years.

4

2

3

2.4.1

| | Cash inflows | | |
|------|--------------|-----------|-----------|
| year | Project X | Project Y | Project Z |
| 1 | 2400 | 5000 | 500 |
| 2 | 2400 | 3000 | 1500 |
| 3 | 2400 | 2000 | 2000 |
| 4 | 2400 | 1500 | 3000 |
| 5 | 2400 | 500 | 5000 |
| 6 | 2400 | 0 | 0 |

Q6(C) The XYZ company is considering three investment A, B, C. Each requires an investment of 4900 Rs and each has economic life of three years and total cash inflow over the period of 6000 Rs. The pattern for each of proposal differs as below-

4

3

3

1.2.3

| year | Annual Cash Inflows | | |
|------|---------------------|------|------|
| | A | B | C |
| 1 | 1000 | 2000 | 3000 |
| 2 | 2000 | 2000 | 2000 |
| 3 | 3000 | 2000 | 1000 |

| Q6(D) | <p>Calculate NPV of each proposal at 10% rate of return</p> <p>Consider the data for two projects (given in the Table) that a construction company is carrying out:</p> <table><tr><th>Description</th><th>Project - X</th><th>Project - Y</th></tr><tr><td colspan="3">All amounts in INR</td></tr><tr><td>Contract amount</td><td>15,00,000</td><td>25,00,000</td></tr><tr><td>Original estimated cost</td><td>18,00,000</td><td>26,00,000</td></tr><tr><td>Billed to date</td><td>13,00,000</td><td>11,00,000</td></tr><tr><td>Payments received to date</td><td>1050000</td><td>1050000</td></tr><tr><td>Costs incurred to date</td><td>750000</td><td>8000000</td></tr><tr><td>Forecasted costs to complete the balance work</td><td>250000</td><td>17,00,000</td></tr><tr><td>Cost paid to date</td><td>700000</td><td>700000</td></tr></table> <p>1. The percentage completion of Project X is _____</p> <p>2. Which of the following statements is TRUE?</p> <p>a) There is an over-billing of 1.5 lakh for Project X</p> <p>b) There is an under-billing of 1.5 lakh for Project X</p> <p>c) There is an over-billing of 3 lakhs for Project Y</p> <p>d) There is an under-billing of 2 lakhs for Project Y</p> <p>3. Let 'P' and 'Q' represent the amount receivable till date, for projects X and Y, respectively. The sum of P and Q (in INR) is _____.</p> | Description | Project - X | Project - Y | All amounts in INR | | | Contract amount | 15,00,000 | 25,00,000 | Original estimated cost | 18,00,000 | 26,00,000 | Billed to date | 13,00,000 | 11,00,000 | Payments received to date | 1050000 | 1050000 | Costs incurred to date | 750000 | 8000000 | Forecasted costs to complete the balance work | 250000 | 17,00,000 | Cost paid to date | 700000 | 700000 | 8 | 4 | 2 | 1.2.3 |
|---|---|-------------|--------------|-------------|--------------------|---------|------|---------------------------|-----------|-----------|-------------------------|-----------|-----------|----------------|-----------|-----------|---------------------------|---------|---------|------------------------|--------|---------|---|--------|-----------|-------------------|--------|--------|---|---|---|-------|
| Description | Project - X | Project - Y | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| All amounts in INR | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Contract amount | 15,00,000 | 25,00,000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Original estimated cost | 18,00,000 | 26,00,000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Billed to date | 13,00,000 | 11,00,000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Payments received to date | 1050000 | 1050000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Costs incurred to date | 750000 | 8000000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Forecasted costs to complete the balance work | 250000 | 17,00,000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Cost paid to date | 700000 | 700000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q7(A) | A contractor had an income of INR 50,000 (after tax) in the year 2020. The depreciation expenses were INR 6,500, and total cash flow was INR 50,000. What happened to the net working capital during the year? | 4 | 2 | 4 | 2.2.4 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q7(B) | For a given project, the contractor has estimated that he would be required to keep an average stock equivalent to INR 20 lakhs. Further, it is also estimated that the average outstanding and average unadjusted advance would be INR 270 lakhs and 60 lakhs, respectively. Estimate the average funds likely to be to be employed for this project if it is known that the contractor would be required to keep an average fixed asset of INR 50 lakhs. | 4 | 1 | 2 | 1.1.3 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q7(C) | <p>Calculate the acid test ratio and current ratio from the given Table:</p> <table><tr><th>Description</th><th>Amount (INR)</th></tr><tr><td>Cash</td><td>1500</td></tr><tr><td>Debtors</td><td>1000</td></tr><tr><td>Total current liabilities</td><td>5000</td></tr></table> <p>Choose the correct answer for acid test ratio and current ratio respectively from the given options</p> <p>A. (0.25:1, 0.25:1)</p> <p>B. (0.5:1, 0.5:1)</p> <p>C. (0.25:1, 0.5:1)</p> | Description | Amount (INR) | Cash | 1500 | Debtors | 1000 | Total current liabilities | 5000 | 4 | 4 | 1 | 1.3.2 | | | | | | | | | | | | | | | | | | | |
| Description | Amount (INR) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Cash | 1500 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Debtors | 1000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Total current liabilities | 5000 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| | | | | | | | | | | | | | | | | | | | |
|----------------------|---|-------------|--------------|---------|-------|----------|------|------|-------|-----------|-----|----------------------|-----|-------|-----|---|---|---|-------|
| | D. (0.5:1, 0.25:1) | | | | | | | | | | | | | | | | | | |
| Q7(D) | <p>Calculate the total liabilities and assets from the given Table</p> <table><tr><td>Description</td><td>Amount (INR)</td></tr><tr><td>Capital</td><td>8000</td></tr><tr><td>Mortgage</td><td>3500</td></tr><tr><td>Land</td><td>11000</td></tr><tr><td>Furniture</td><td>500</td></tr><tr><td>Outstanding expanses</td><td>900</td></tr><tr><td>Stock</td><td>990</td></tr></table> | Description | Amount (INR) | Capital | 8000 | Mortgage | 3500 | Land | 11000 | Furniture | 500 | Outstanding expanses | 900 | Stock | 990 | 4 | 3 | 5 | 2.2.4 |
| Description | Amount (INR) | | | | | | | | | | | | | | | | | | |
| Capital | 8000 | | | | | | | | | | | | | | | | | | |
| Mortgage | 3500 | | | | | | | | | | | | | | | | | | |
| Land | 11000 | | | | | | | | | | | | | | | | | | |
| Furniture | 500 | | | | | | | | | | | | | | | | | | |
| Outstanding expanses | 900 | | | | | | | | | | | | | | | | | | |
| Stock | 990 | | | | | | | | | | | | | | | | | | |
| Q7(E) | <p>Choose the correct answer for total liabilities and assets respectively from the given options</p> <p>A. 12000, 12890</p> <p>B. 12400, 12400</p> <p>C. 12490, 12400</p> <p>D. 12400, 12490</p> | 4 | 4 | 2 | 1.2.3 | | | | | | | | | | | | | | |



Bharatiya Vidya Bhavan's
Sardar Patel College of Engineering

(A Government Aided Autonomous Institute)
Munshi Nagar, Andheri (West), Mumbai – 400058



End Sem Exam April 2022

Program: M. Tech. Construction Management Sem I Duration: 3 hr

Course code: MTCM103

Maximum Marks: 20

Name of the Course: Advanced Construction Techniques

Semester: I

Instructions:

1. Attempt any 5 questions.
2. Neat diagrams must be drawn wherever necessary.
3. Figures to the right side indicate full marks.
4. Assume Suitable data if necessary and state it clearly

| Q. No. | Questions | Points | CO | BL | PI |
|--------|---|--------|-----|-----|-------|
| 1a | Discuss advantage of pre-engineered building | 05 | CO2 | BL1 | 1.3.1 |
| 1b | Explain in detail soil exploration for bridge construction site | 10 | CO1 | BL2 | 1.3.1 |
| 1c | Discuss issues and challenges faced during Teesta dam construction project. | 05 | CO3 | BL3 | 1.3.1 |
| 2a | Discuss Causes of landslide and precautionary measures for the same | 10 | CO1 | BL1 | 1.3.1 |
| 2b | State the effect of inadequate or improper soil exploration on any construction project. | 05 | CO2 | BL1 | 1.3.1 |
| 2c | Discuss sprayed concrete along with its application. | 05 | CO2 | BL1 | 2.1.2 |
| 3a | Discuss in detail different methods of drilled shaft constructions | 10 | CO1 | BL2 | 1.3.1 |
| 3b | Differentiate PEBs vs Conventional steel building. | 10 | CO1 | BL1 | 1.3.1 |
| 4a | Elaborate on the advantages and limitations of precast and pre-stressed components of buildings | 10 | CO2 | BL1 | 2.1.2 |
| 4b | Define micro tunneling and discuss its advantages | 05 | CO2 | BL1 | 2.1.2 |

| | | | | | |
|----|--|----|-----|-----|-------|
| 4c | Explain about low cost roads. | 05 | CO2 | BL1 | 1.3.1 |
| 5a | Discuss slip form method of construction. | 05 | CO2 | BL1 | 1.3.1 |
| 5b | Discuss applications of GGBs. | 05 | CO2 | BL2 | 2.1.2 |
| 5c | You have been assigned responsibility of construction of Smart city project, wherein it is proposed to use sustainable materials, which materials will you prefer for this project, explain in detail. | 10 | CO3 | BL3 | 3.1.6 |
| 6a | Explain in detail the various types of pile foundations. | 08 | CO1 | BL1 | 1.3.1 |
| 6b | Discuss the need of recycling of material along with purpose of recycled aggregates. | 06 | CO2 | BL2 | 1.3.1 |
| 6c | Discuss different methods of boring. | 06 | CO1 | BL1 | 2.1.2 |
| 7a | Elaborate on various types of patented formworks with their advantages and disadvantages. | 10 | CO2 | BL2 | 1.3.1 |
| 7b | Define and discuss pre-stressing along with its type and advantages | 06 | CO1 | BL1 | 1.3.1 |
| 7c | Brief about safety precautions to be taken during geotechnical exploration. | 04 | CO1 | BL2 | 1.3.1 |

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END SEMESTER EXAMINATION

| | | | |
|-------------|---------------------------------|-------------------------------------|--|
| Programme | MTech Structural Engineering | MTech Construction Management | MTech Power Sytems and Power Electronics |
| Course Code | MC-PG01 | MC-PG01 | MC-MTPX101 |

Subject : Research Methodology and IPR ✓

Total Marks :100

Class: MTech, Sem:I,

Duration : 3 Hours

25th April 2022

- Question 1 is compulsory
- Solve Any Four Questions from the remaining
- Answers to all sub questions **must be** grouped together
- Figures to the right indicate full marks
- Assume suitable data wherever necessary

| SN | Question statement | Points | Module | CO |
|-----|---|--------|-------------------------|-------------|
| Q1 | Explain the following with suitable examples A. Guidelines for writing a Literature survey for a paper A. Statistical Hypothesis Test Procedures and the Criminal Trial Analogy B. Types of IPR and their significance C. Scatter Plot and Co-relation | 20 | M1,M3, M4, M6, M7 | CO3, CO4 |
| Q2A | A population is divided into four strata so that $N_1 = 8500$, $N_2 = 4500$ and $N_3 = 9500$, $N_4 = 11500$ Respective standard deviations are: $s_1=12$, $s_2=14$, $s_3=7$, $s_4=6$. Costs in rupees to collect the strata are $C_1= 9000$, $C_2=5000$, $C_3=10000$, $C_4= 12000$. How should a sample of size $n = 98$ be allocated to the four strata, if we want optimum allocation using Cost Optimal Disproportionate sampling design? | 10 | M3 | CO2 |
| Q2B | Researcher conducted experimental investigations on concrete cubes, to study the influence of fly ash, GGBS and glass waste powder (GWP) individually, on the compressive strength of concrete. The cubes were casted for M30 grade of concrete and by random sampling method, tested after 28 days curing. For cubes in Group I, 30% fly ash was added, for Group II, 30% GGBS was added and in Group III, 30% GWP was added. The 28 days compressive strengths of cubes in N/mm^2 are given below. Check whether the mean compressive strength of the 3 different groups is same or not. Group I – 35, 29, 34, 35, 27, 29 Group II – 33, 29, 30, 29, 33 Group III – 34, 28, 29, 32, 33, 27, 28 | 10 | M5 | CO2 |

| | | | | | | | | | | | | | | | | | | | | |
|---------------------------|---|------------------|------------------------|------------------|-------|------------|--------------|-----|-----|----------------|-----|---------------------------|-----|-------|-----|-----|-----|--------|----------|-----|
| Q3A | <p>A data of 450 construction Projects was reviewed to know association between type of construction project and success of construction project. The response by Type of Project are as follows. At $\alpha = 0.05$ do these data suggest an association between Type of Project and being successful?</p> <table><tr><td></td><td>International Projects</td><td>Domestic Project</td><td>Total</td></tr><tr><td>Successful</td><td>46</td><td>88</td><td>134</td></tr><tr><td>Not Successful</td><td>184</td><td>179</td><td>363</td></tr><tr><td>Total</td><td>230</td><td>267</td><td>497</td></tr></table> | | International Projects | Domestic Project | Total | Successful | 46 | 88 | 134 | Not Successful | 184 | 179 | 363 | Total | 230 | 267 | 497 | 10 | M5 | CO2 |
| | International Projects | Domestic Project | Total | | | | | | | | | | | | | | | | | |
| Successful | 46 | 88 | 134 | | | | | | | | | | | | | | | | | |
| Not Successful | 184 | 179 | 363 | | | | | | | | | | | | | | | | | |
| Total | 230 | 267 | 497 | | | | | | | | | | | | | | | | | |
| Q3B | <p>Manufacturer wants to test on the basis of sample size 35 determinations and at 0.05 and 0.01 levels of significance whether the thermal conductivity of a certain kind of plate is 0.34 units, as has been claimed. The mean of sample is 0.343. From the information gathered in similar studies , we can expect that the variability of such determinations is given by $\sigma = 0.01$. Assume any suitable data if necessary.</p> | 10 | M1, M5 | CO1, CO2 | | | | | | | | | | | | | | | | |
| Q4A | <p>A maker of golf shirts has been tracking the relationship between sales and advertising dollars. Use linear regression to find out what sales might be if the company invested \$68,000 in advertising next year.</p> <table><tr><td></td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>Sales \$ (y)</td><td>150</td><td>171</td><td>170</td><td>178</td></tr><tr><td>Advertisement expenditure</td><td>42</td><td>62</td><td>60</td><td>65</td></tr></table> | | 1 | 2 | 3 | 4 | Sales \$ (y) | 150 | 171 | 170 | 178 | Advertisement expenditure | 42 | 62 | 60 | 65 | 10 | M1, M5 | CO1, CO2 | |
| | 1 | 2 | 3 | 4 | | | | | | | | | | | | | | | | |
| Sales \$ (y) | 150 | 171 | 170 | 178 | | | | | | | | | | | | | | | | |
| Advertisement expenditure | 42 | 62 | 60 | 65 | | | | | | | | | | | | | | | | |
| Q4B | State the characteristics of Good research Problem | 10 | M1 | CO1 | | | | | | | | | | | | | | | | |
| Q5A | Differentiate between Research Paper and Review paper. State the Guidelines to write the research article. | 10 | M2, M3 | CO1, CO2 | | | | | | | | | | | | | | | | |
| Q5B | Differentiate between Qualitative and Quantitative Research | 10 | M1, M2 | CO1 | | | | | | | | | | | | | | | | |
| Q6A | State the difference between Copyright Patent and Trademark | 10 | M5 | CO3, CO4 | | | | | | | | | | | | | | | | |
| Q6B | Draw the flow chart and explain the procedure to receive the patent. | 10 | M4, M6 | CO3, CO4 | | | | | | | | | | | | | | | | |
| Q7 | <p>Explain the following with suitable examples</p> <ul style="list-style-type: none">• Null Hypothesis and Alternate Hypothesis• Type 1 error and Type 2 error• Test Statistics• Confidence Level and p value• Limitations and advantages of Hypothesis Test• Rejection Region• Left Tail Test and Right Tail Test• One Tail Test and Two Tail Test | 20 | M1 | CO1 | | | | | | | | | | | | | | | | |

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Munshi Nagar, Andheri (W) Mumbai – 400058



End Semester – April 2022 Examinations

M. Tech in Civil Engg in 100 Marks. mgt Sem I

Program: F Y M.Tech

Duration: 3 Hours

Course Code: AU-PG 01

Maximum Points: 100

27/4/22

Course Name: Project Planning and Management

Semester: I

Notes: 1. Answer any five questions.

2 All questions carry 20 points.

| Q.No. | Questions | Points | CO | BL | PI |
|-------|---|--------|----|----|--------|
| 1 | 1.1 What are the attributes or skills that a Project Manager should have? | 10 | 2 | 2 | 2.1.2 |
| | 1.2 Explain the three Project Quality Management processes | 10 | 2 | 2 | 11.3.1 |
| 2 | 2.1 List out ten steps, in sequence, for the preparation of Civil Structural, Architectural Tender specification. | 10 | 1 | 2 | 11.3.1 |
| | 2.2 Why is it important to issue a Civil, Structural, Architectural design basis for the project? List ten of the most important design requirements that should be contained in the design basis. | 10 | 1 | 2 | 3.1.6 |
| 3 | 3.1 Explain the three fundamental components of a computer model used for structural analysis. What are the three stages in the process of computer analysis? | 10 | 3 | 2 | 6.1.1 |
| | 3.2 List out at least ten steps, in sequence, in the designing of a complex plant steel structure | 10 | 3 | 2 | 6.1.1 |
| 4 | 4.1 What is the difference in approach between Limit state (Load Factor) design and working stress design? In Limit state design what are the two key load conditions? What are the checks for each of these load conditions? | 10 | 3 | 4 | 3.4.1 |



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End Semester – April 2022 Examinations

| | | | | | |
|---|---|----|---|---|--------|
| | 4.2 Define degrees of freedom. Specify the degrees of freedom and the equilibrium conditions for a rigid body in two dimensions. | 5 | 2 | 3 | 1.2.1 |
| | 4.3 Explain Strength, Stiffness, Stability and Ductility at the element and system levels. | 5 | 2 | 3 | 11.3.2 |
| 5 | Explain any three top emerging trends which are impacting the Construction industry today. | 10 | 1 | 2 | 3.3.1 |
| | 5.2 In five areas, explain how structural engineers can overcome the challenges faced by the profession. | 10 | 1 | 2 | 2.4.2 |
| 6 | List out atleast ten points defining the scope of a contour and traverse survey for a project plot. | 10 | 3 | 4 | 2.4.2 |
| | 6.2 Why is quantity/cost monitoring important during execution of a CSA item-rate contract? How is quantity monitoring done during the project execution? | 5 | 3 | 5 | 1.3.1 |
| | 6.3 What are the main objectives of constructability reviews | 5 | 4 | 2 | 11.3.1 |
| 7 | 7.1 In a soil investigation specification, describe five field tests you would specify along with the soil parameter each test would measure | 10 | 3 | 2 | 3.2.2 |
| | 7.2 List six soil properties and four recommendations for pile foundations that you would ask for in the final geo-technical report. | 10 | 2 | 3 | 3.4.2 |